

Partial Contracts

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joint with

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O. Hart and J. Moore:

“Agreeing Now to Agree Later:
Contracts that Rule Out but do not Rule In”,
mimeo, September 2005

“Contracts as Reference Points”,
mimeo, July 2006

O. Hart and J. Moore:

“Agreeing Now to Agree Later:
Contracts that Rule Out but do not Rule In”,
mimeo, September 2005 (PAPER 1)

“Contracts as Reference Points”,
mimeo, July 2006 (PAPER 2)

Partial Contracts

or

More is Less?

or

Moore is Less?

Other themes to watch for:

- flexibility vs. rigidity
- money is taken “off the table” first:
 - { start by agreeing the price
 - { later agree other elements of contracte.g. employment contract
- nature of employment contract:
 - do bosses have power?
- efficiency wages/Keynes

Buyer/Seller model:

Bishop (B)

Soprano (S)

risk neutral

no wealth constraints

date 0

date $\frac{1}{2}$

date 1



competitive
market

lock-in

bilateral
monopoly

B and S
meet and
contract

uncertainty
resolved

B and S
trade

2 states, distinguished by colour:

Lilac State prob $\frac{1}{2}$

Red State prob $\frac{1}{2}$

B and S contract over:

musical programme and price

2 states, distinguished by colour:

Lilac State prob $\frac{1}{2}$

Red State prob $\frac{1}{2}$

B and S contract over:

music/price ●

music/price ●



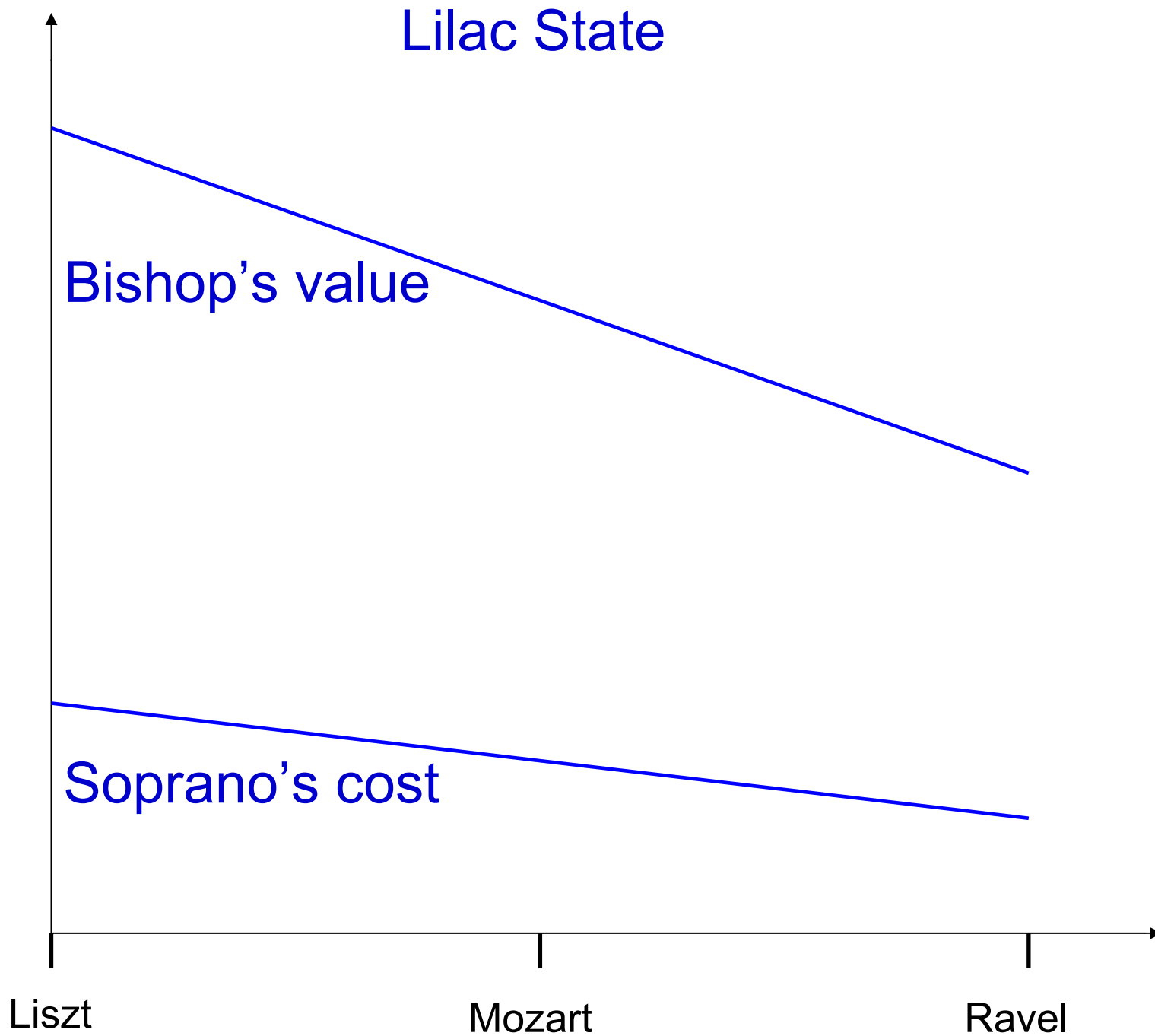
Euros

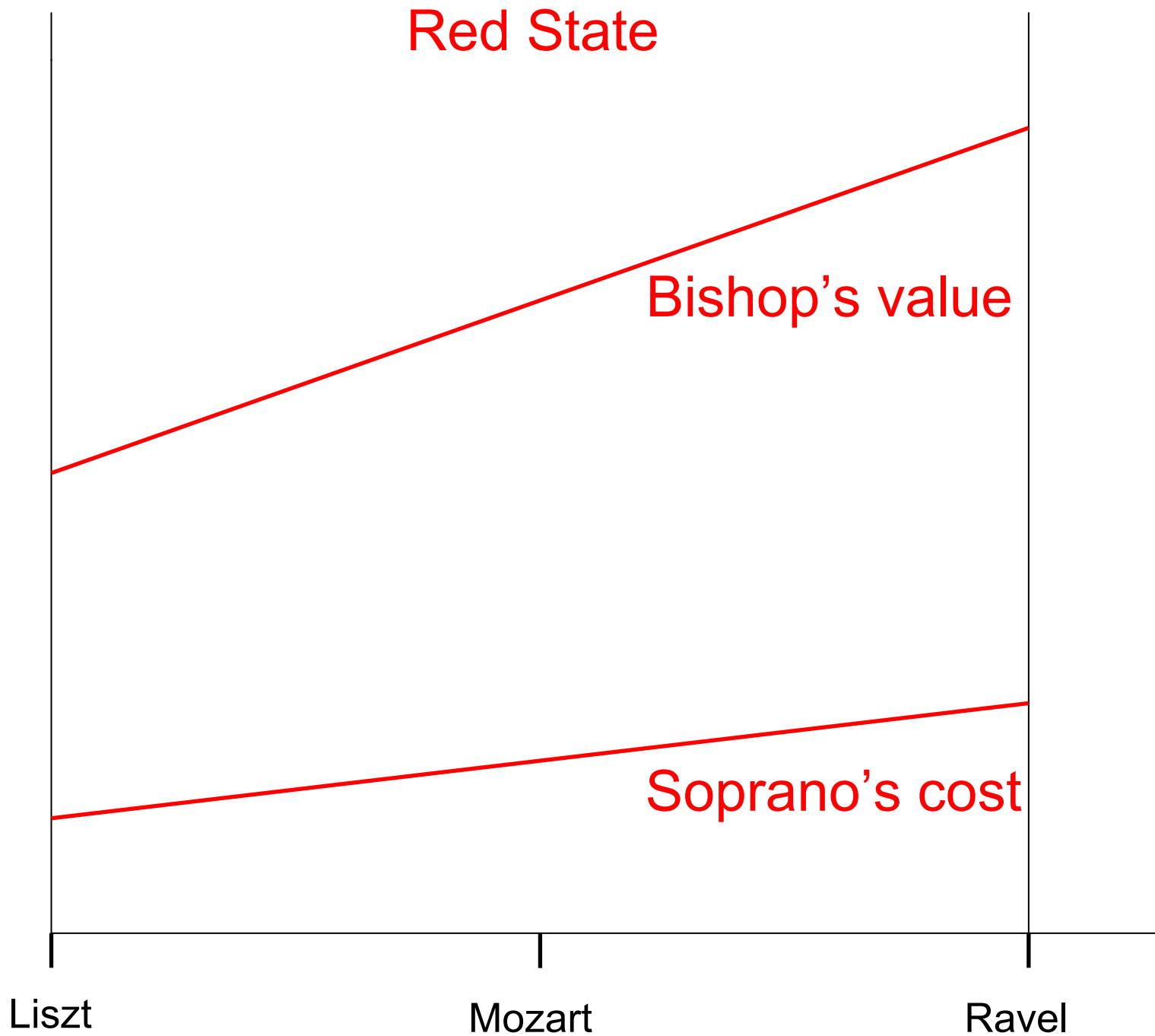


Liszt

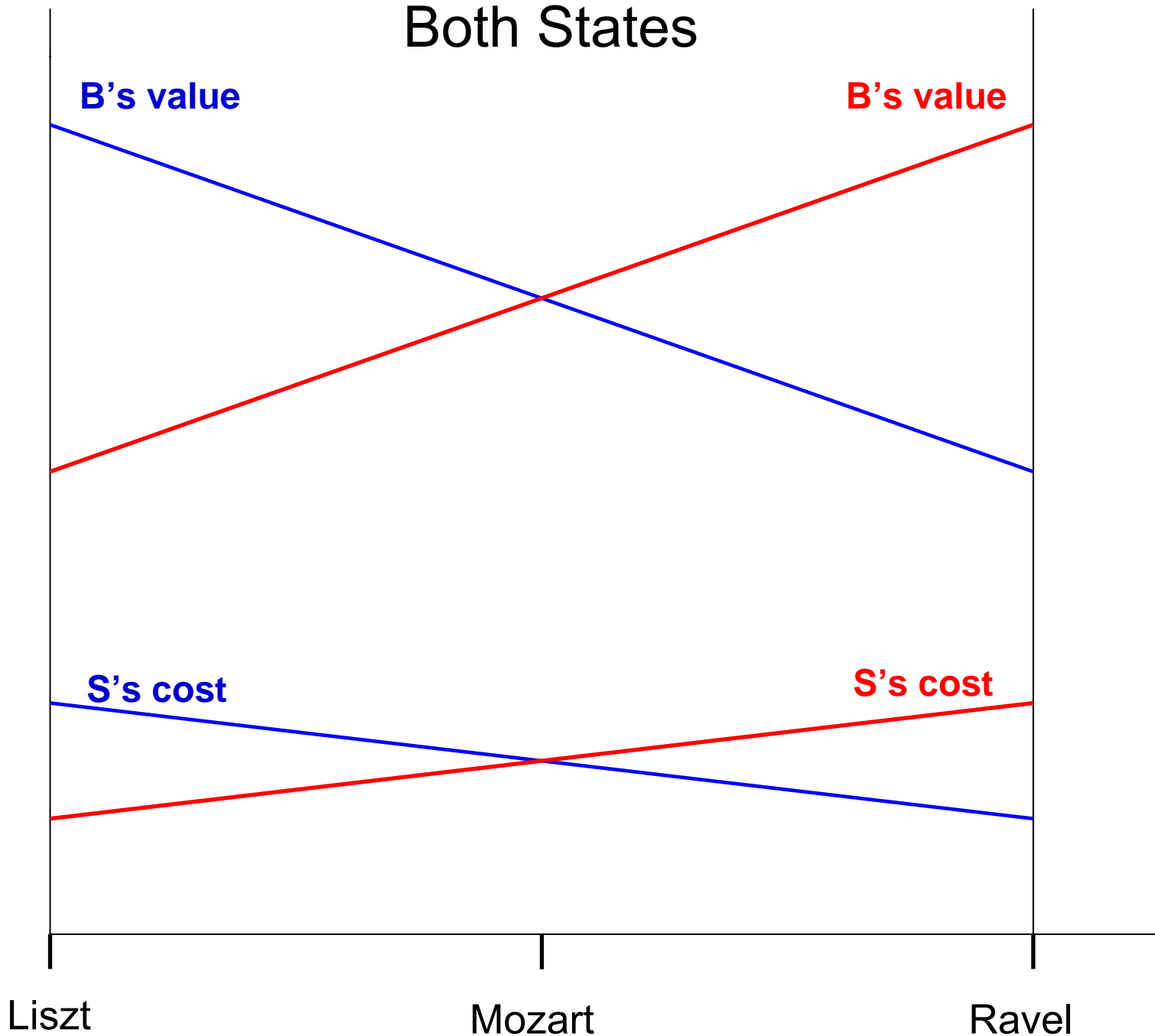
Mozart

Ravel

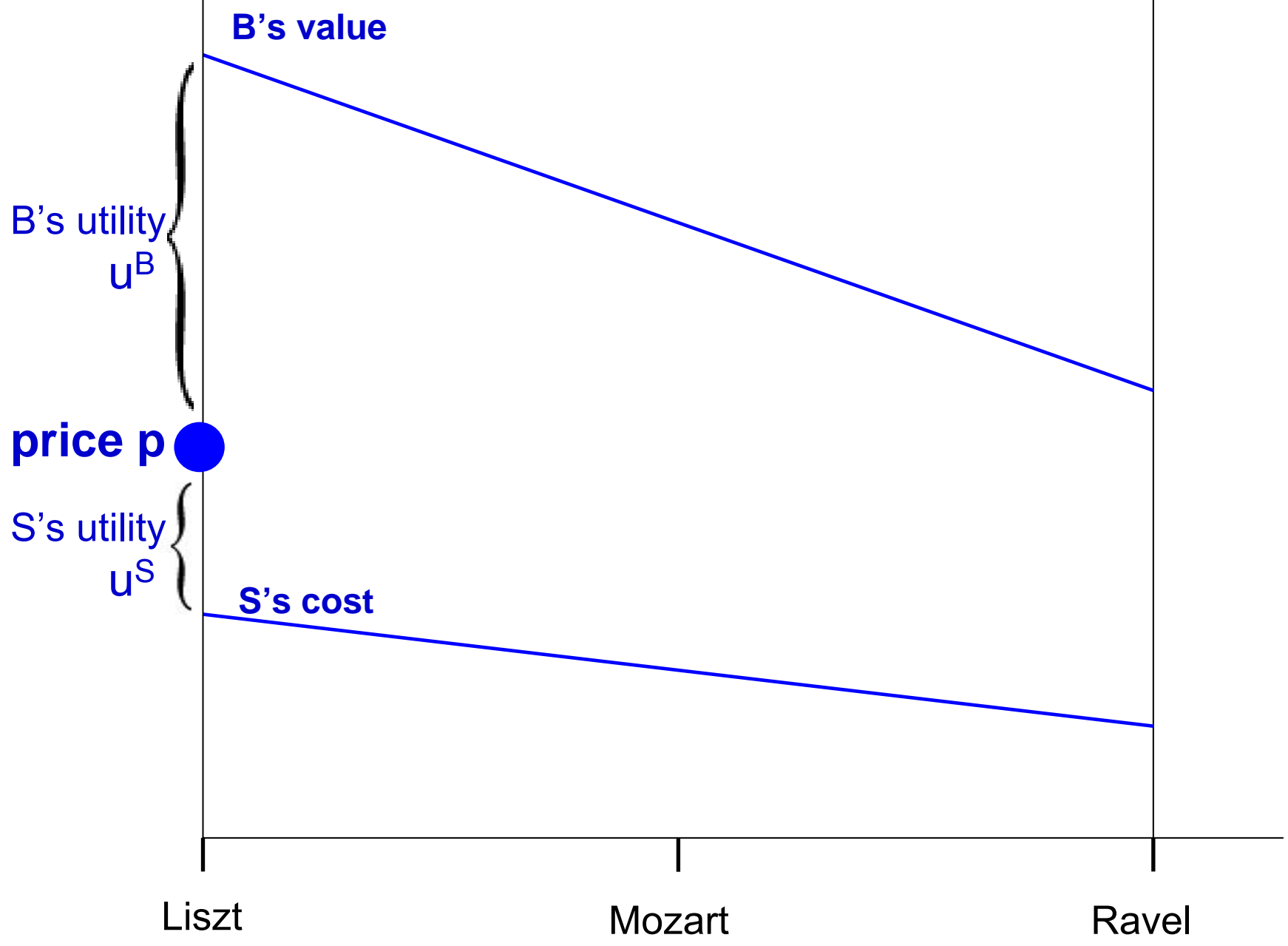




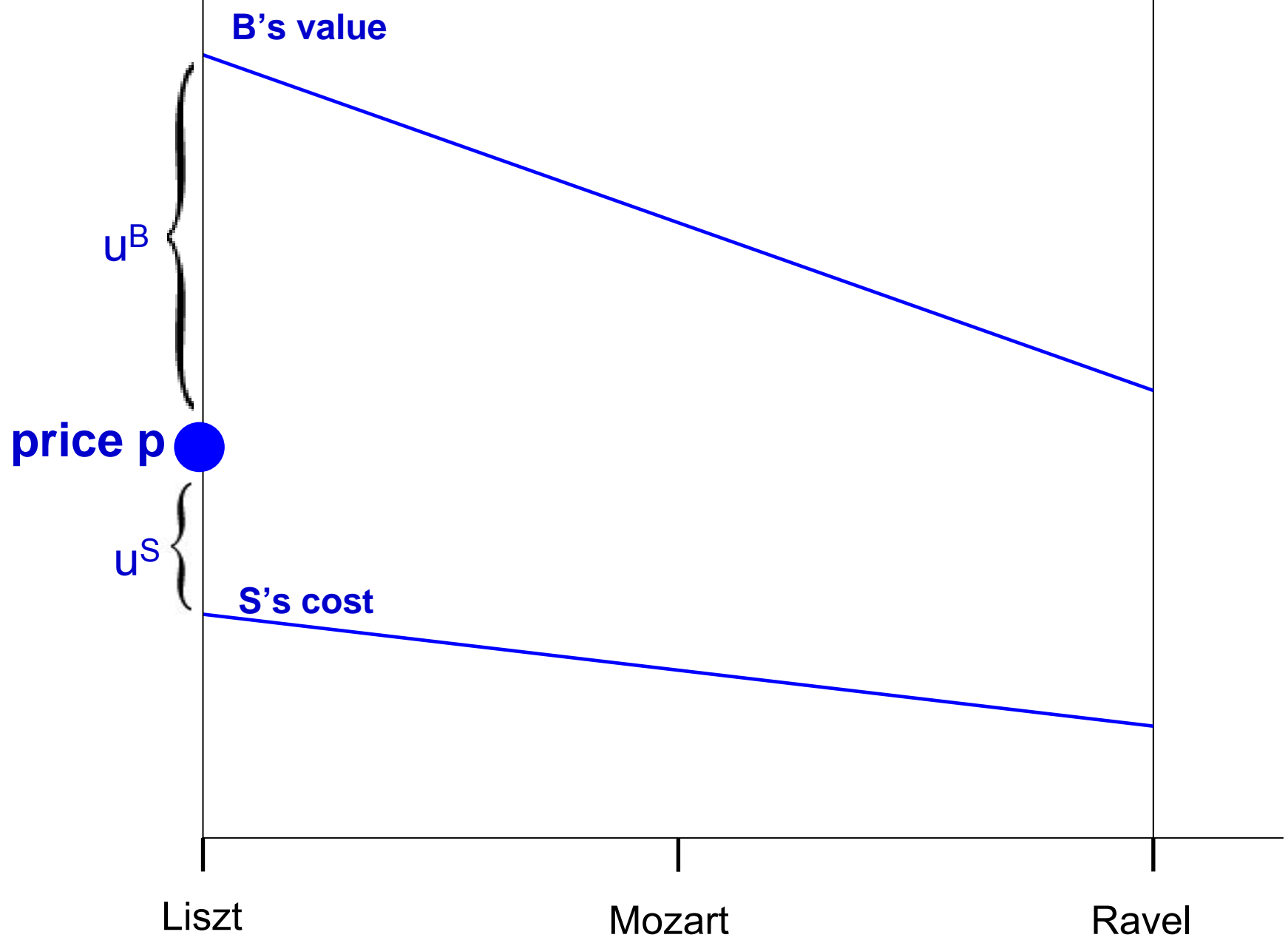
Both States



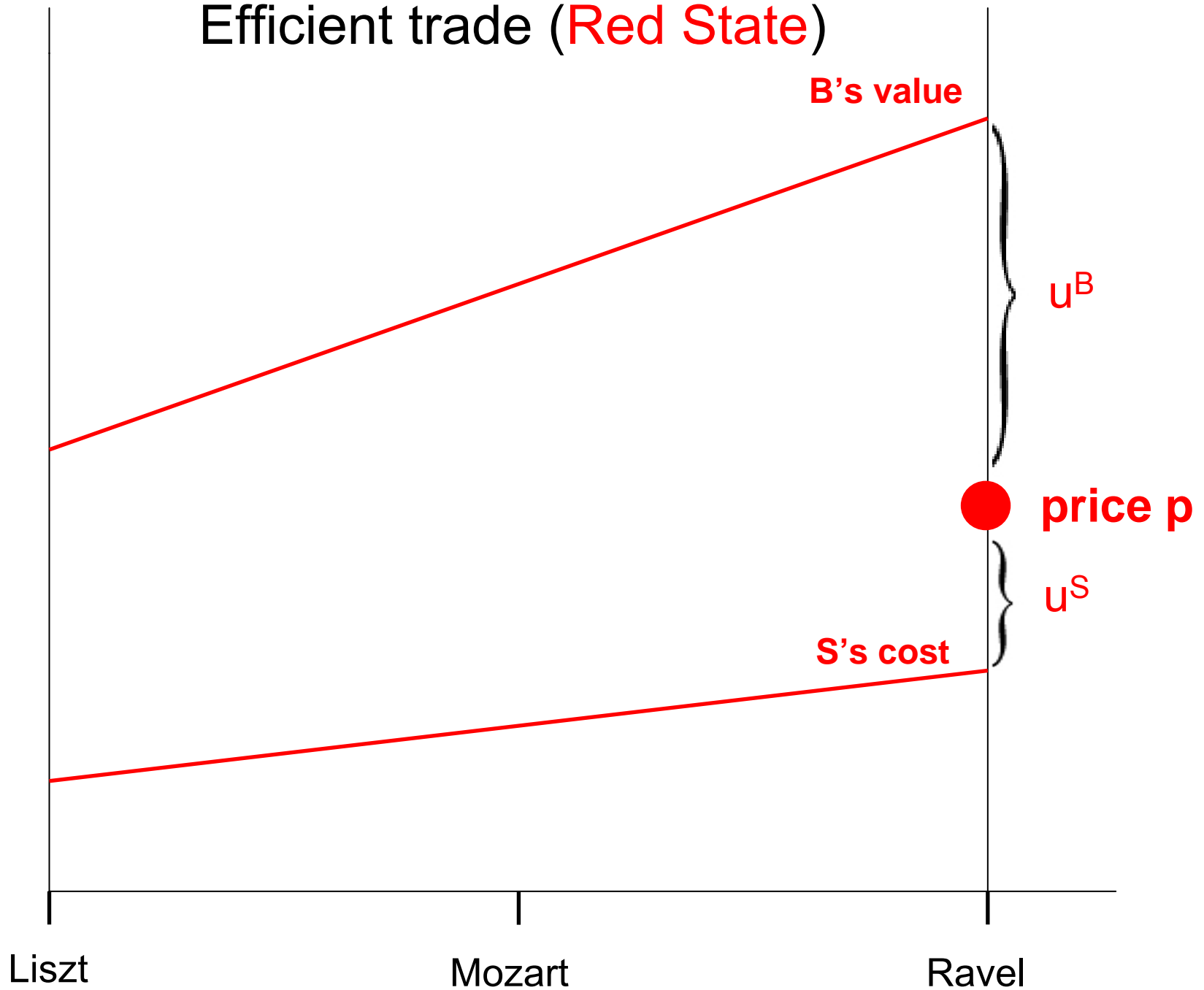
Efficient trade (Lilac State)



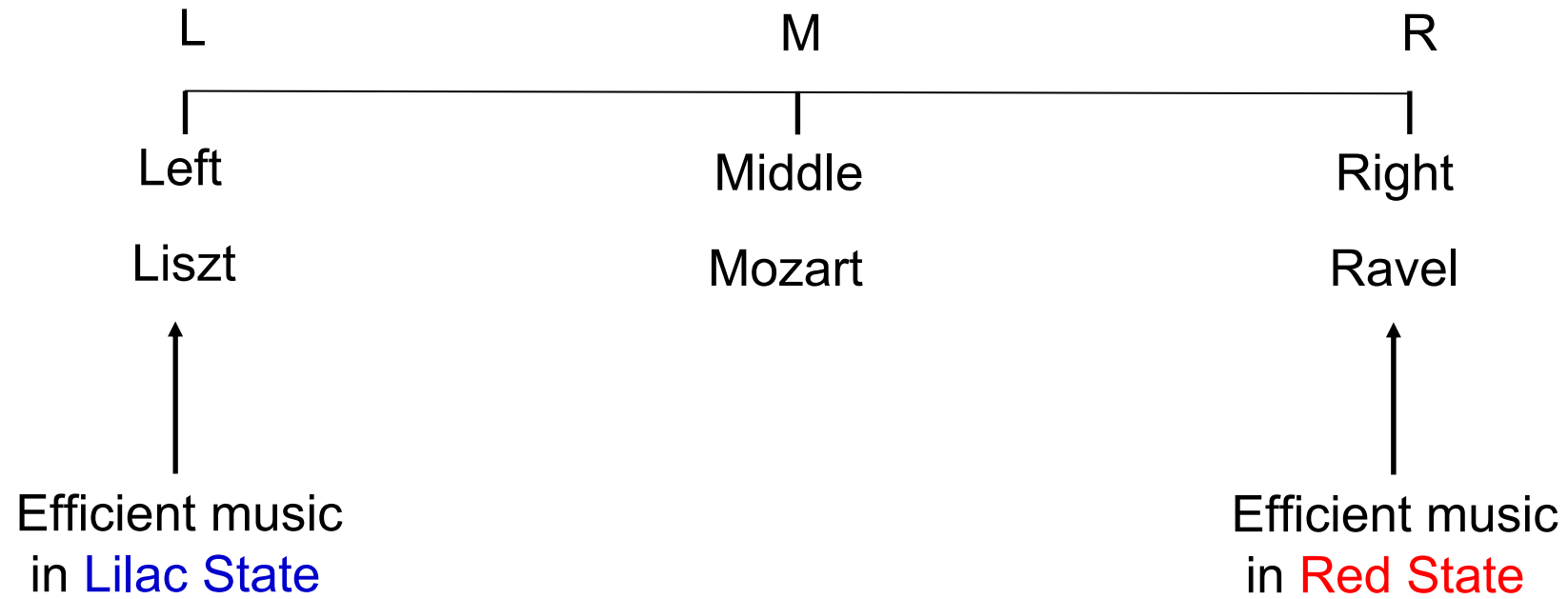
Efficient trade (Lilac State)

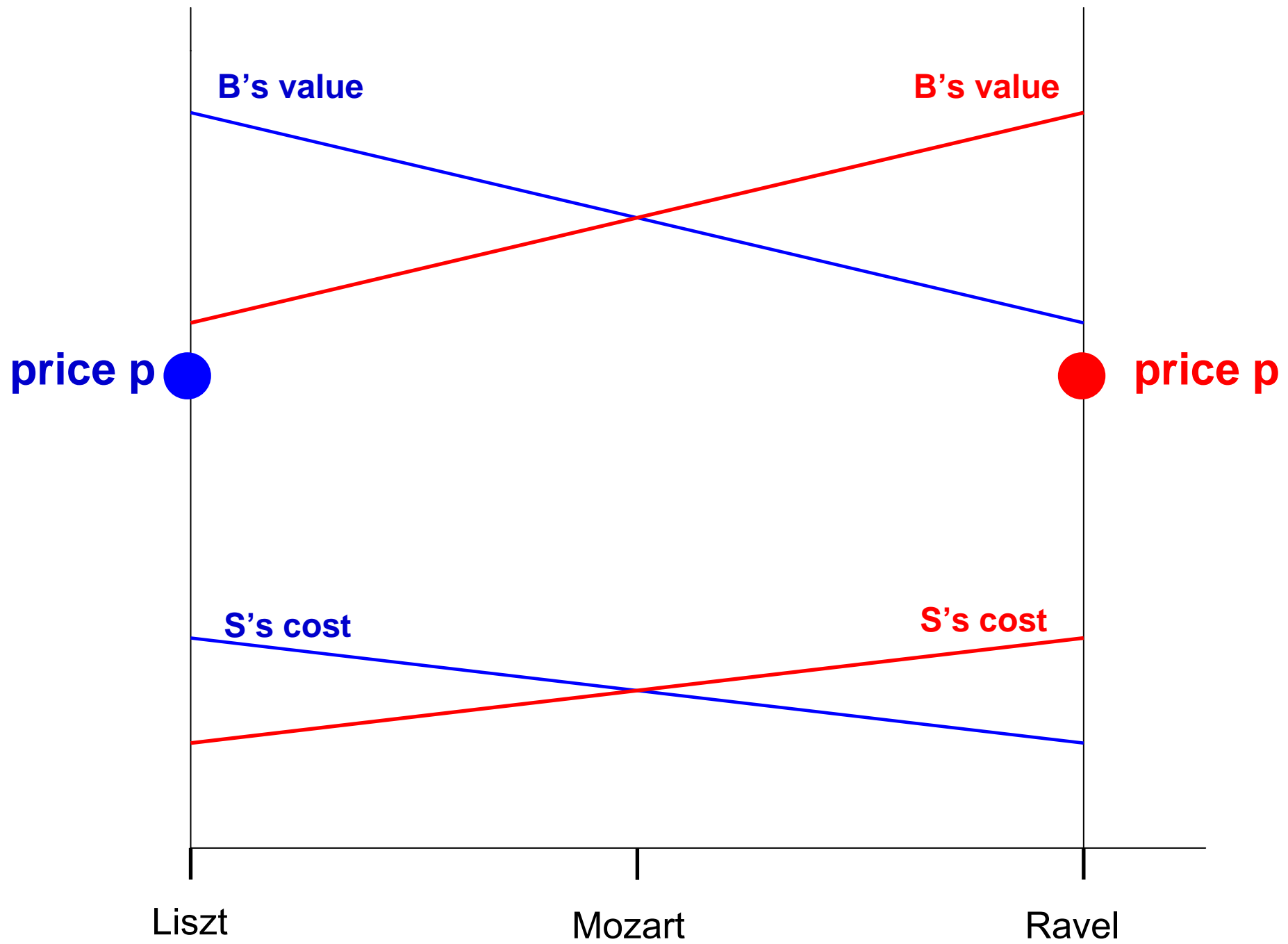


Efficient trade (Red State)

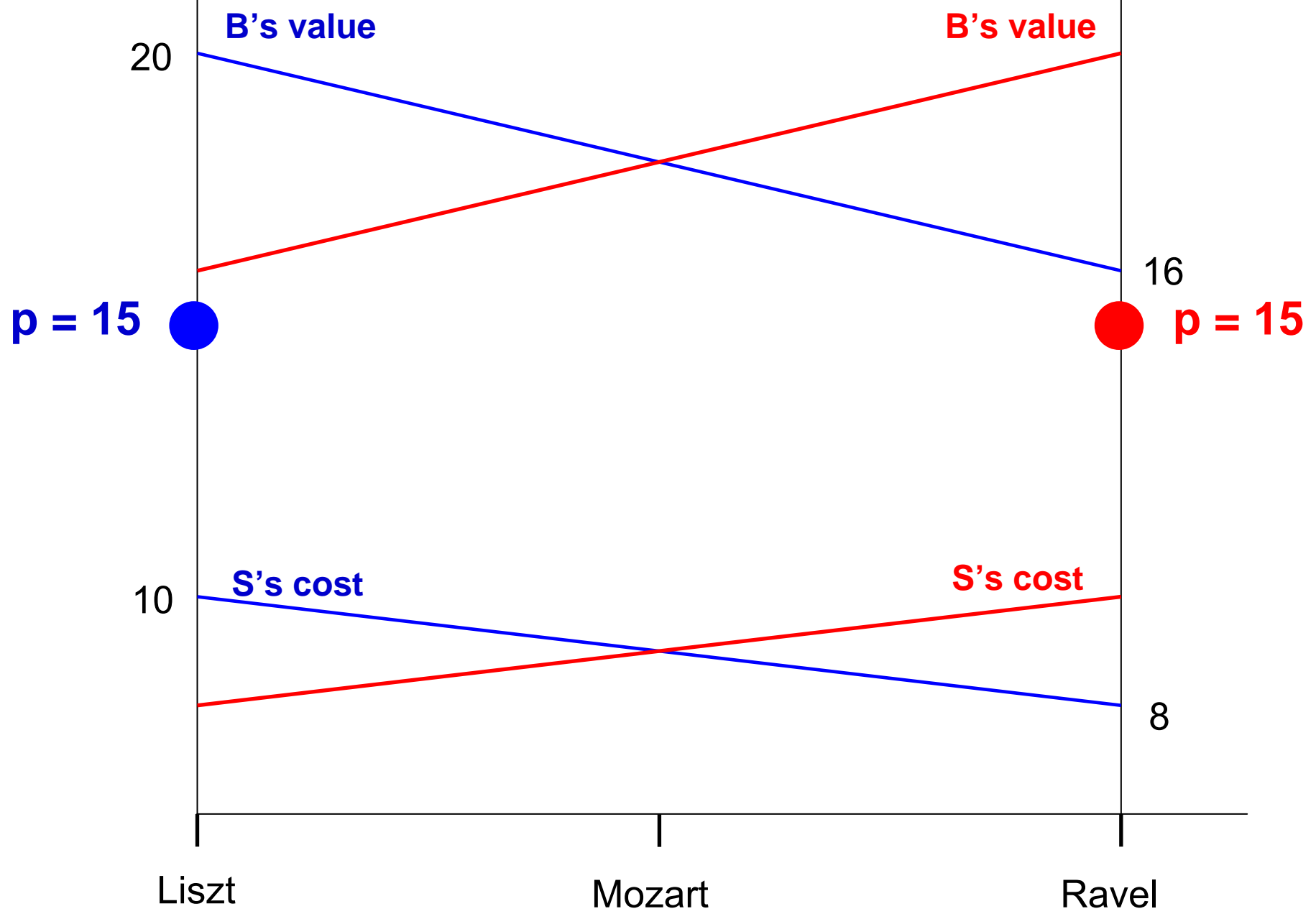


Mnemonic:





Numerical Example



Problem: Judges are colour blind

=> states are non-verifiable at date 1

=> contracts cannot be state-contingent

B and S are not colour blind

=> they observe state at date 1

(no asymmetric information)

Question: What can be implemented?

Maskin mechanisms:

each party announces state

agree => implement desired music/price

disagree => implement something cunning

mechanism designed so that in equilibrium

both parties want to announce true state

mechanism written
into contract:

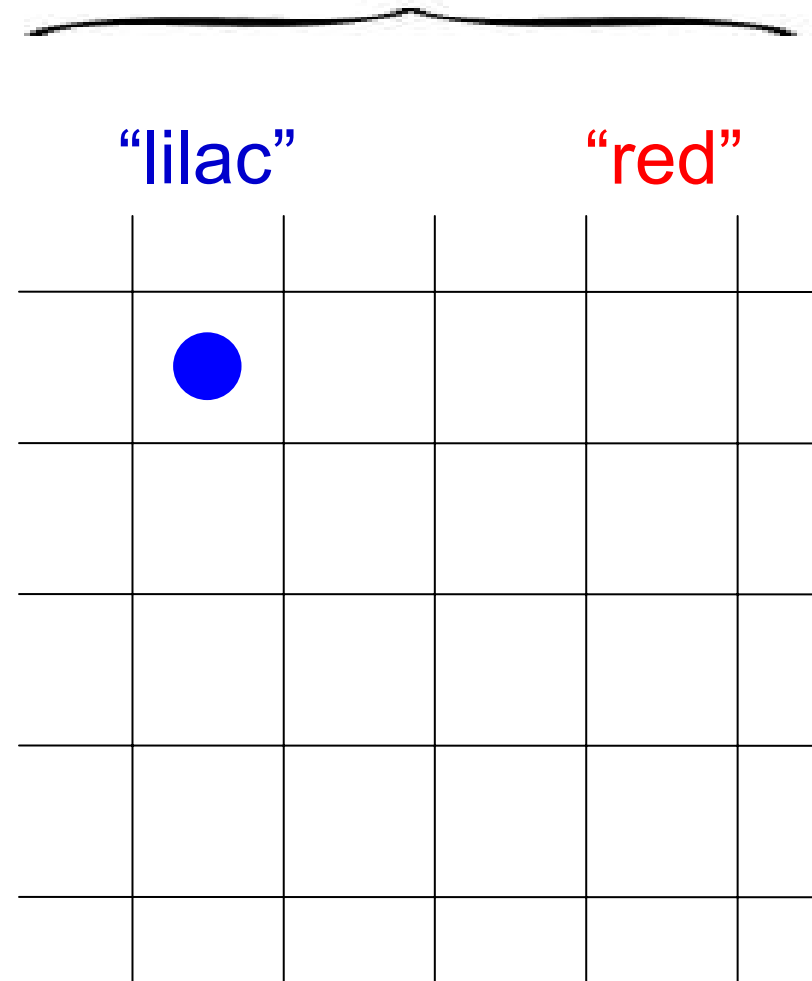
Lilac State

Bishop
announces

“lilac”

“red”

Soprano
announces



mechanism written
into contract:

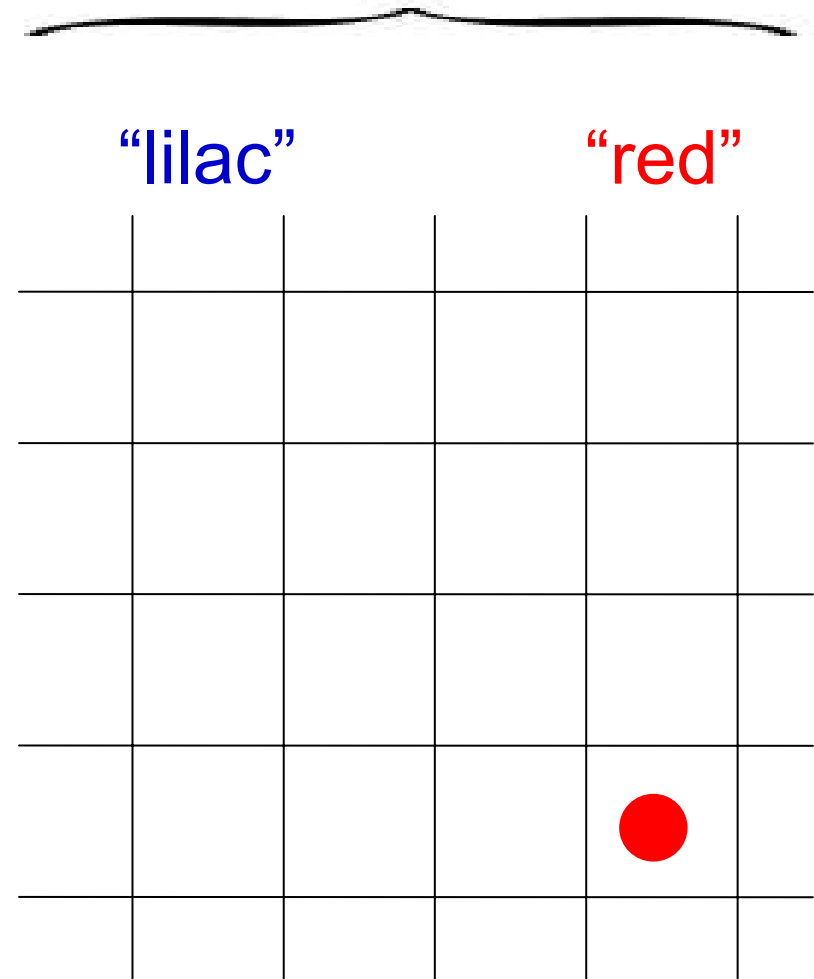
Red State

Bishop
announces

“lilac”

“red”

Soprano
announces



mechanism written
into contract:

Soprano
announces

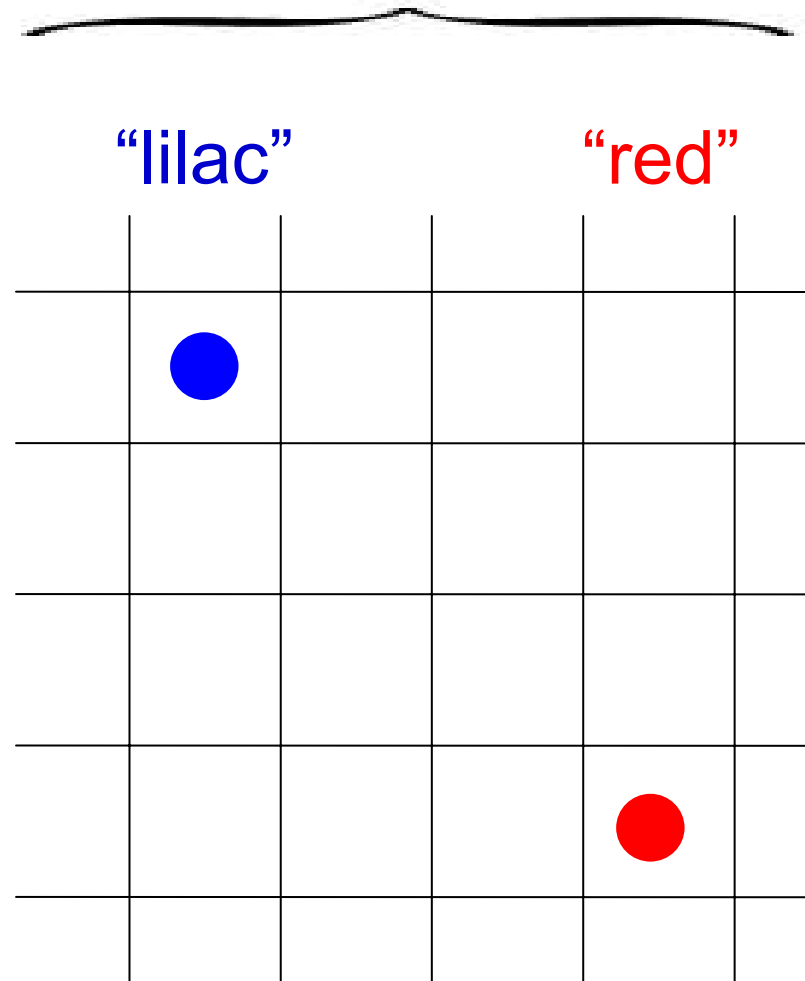
“lilac”

“red”

“lilac”

Bishop
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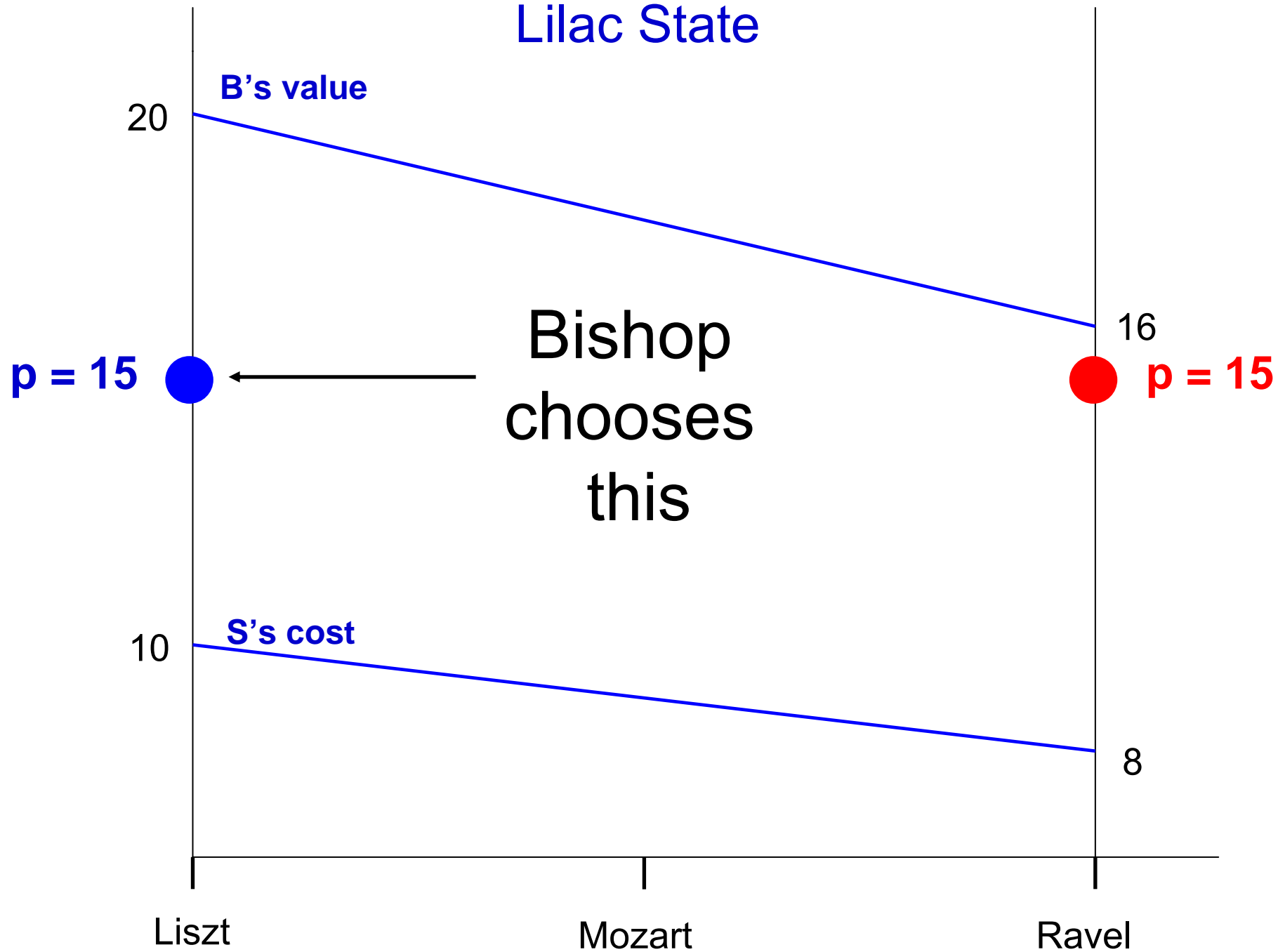
“red”

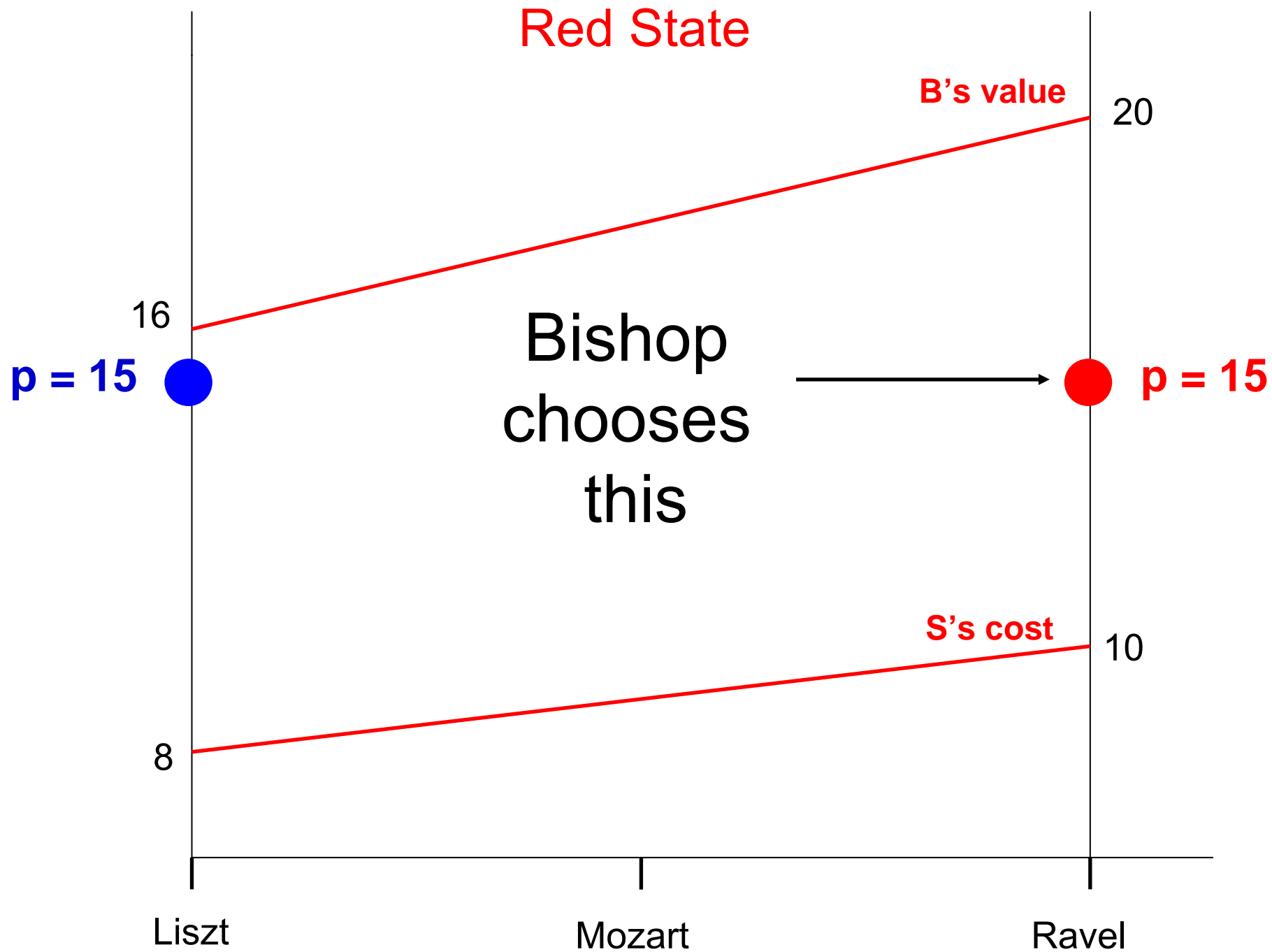


In our Bishop/Soprano model, there is a very simple Maskin mechanism:

fixed price ($p = p$)
Bishop chooses music

Lilac State





In our Bishop/Soprano model, there is a very simple Maskin mechanism:

fixed price ($p = p$)
Bishop chooses music

Maskin mechanisms are often sophisticated

Are we missing something?

When writing a contract,

could more sophistication
yield less welfare?

More is less?

Partial Contracting

Some aspects of performance are
non-contractible,
beyond the reach of the law

Consummate vs. Perfunctory
performance

Bishop may have legal right to choose music, but Soprano will be aggrieved if she feels she is being treated “unfairly

Bishop may have legal right to choose music, but Soprano will be aggrieved if she feels she is being treated “unfairly”, and retaliate by singing badly

Bishop may have legal right to choose music, but Soprano will be aggrieved if she feels she is being treated “unfairly”, and retaliate by singing badly (assume she is indifferent between singing well and badly)

Judge can determine whether Liszt, Mozart, or Ravel was actually sung,

but Judge cannot adjudicate how well the music was sung

What is “unfair” treatment?

Let us assume that the Soprano feels entitled to the music/price pair that maximises the Nash product

$$u^B \times u^S$$

Unless the Soprano gets this utility u^S , she will retaliate by singing badly

Crucial assumption (PAPER 1):

B and S have a common view of what is fair

Bishop also feels entitled to the music/price pair that maximises the Nash product

$$u^B \times u^S$$

Unless B gets this utility u^B , he will retaliate
– by poisoning the peanuts

Crucial assumption (PAPER 1):

B and S have a common view of what is fair

Bishop also feels entitled to the music/price pair that maximises the Nash product

$$u^B \times u^S$$

Unless B gets this utility u^B , he will retaliate – by poisoning the peanuts, or by putting her up in the Youth Hostel not the Ritz

All this scope for retaliation

=> mechanisms don't have any bite

e.g. even if B has the right to choose music,
it is a right in name only

Fortunately, B and S agree on what is fair
(not true in PAPER 2!)

All this scope for retaliation

=> mechanisms don't have any bite

e.g. even if B has the right to choose music,
it is a right in name only

Fortunately, B and S agree on what is fair

=> their choice of outcome is "Coasian"

Regardless of any formal mechanism that might have been stipulated in the contract, at date 1 the parties are in effect (Nash) bargaining over some

set C

of music/price pairs

Contract design at date 0 amounts to no more than the specification of C

Soprano

Bishop

B and S bargain over the set C of outcomes
in this matrix

Soprano

Bishop

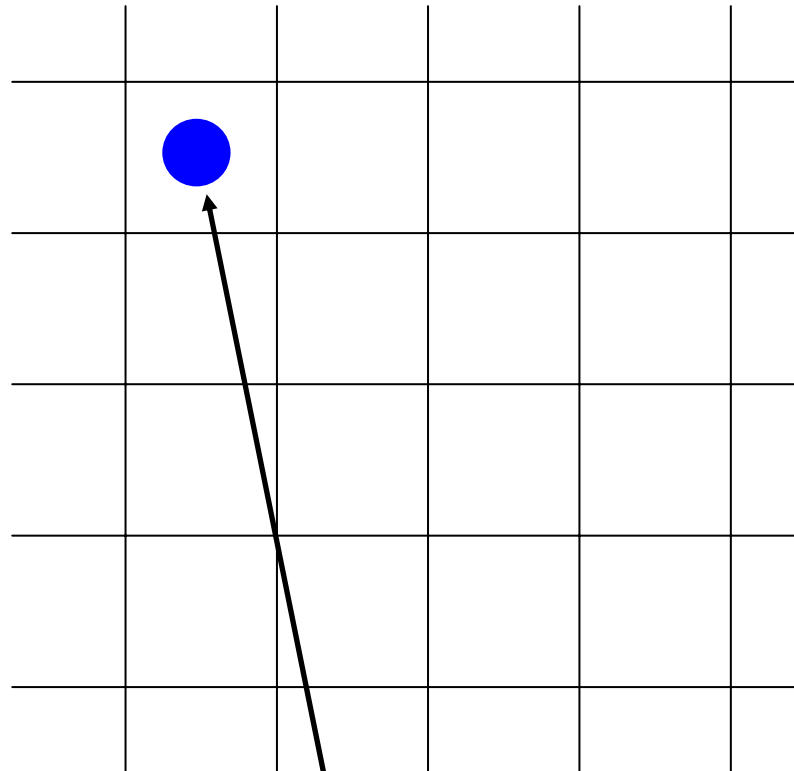
A 5x5 grid representing a bargaining matrix. The grid is composed of 5 columns and 5 rows of empty cells, defined by 6 vertical and 6 horizontal lines. The label 'Soprano' is positioned above the grid, and 'Bishop' is positioned to the left of the grid.

B and S bargain over the set C of outcomes in this matrix (no renegotiation, to outside C)

Lilac State

Soprano

Bishop

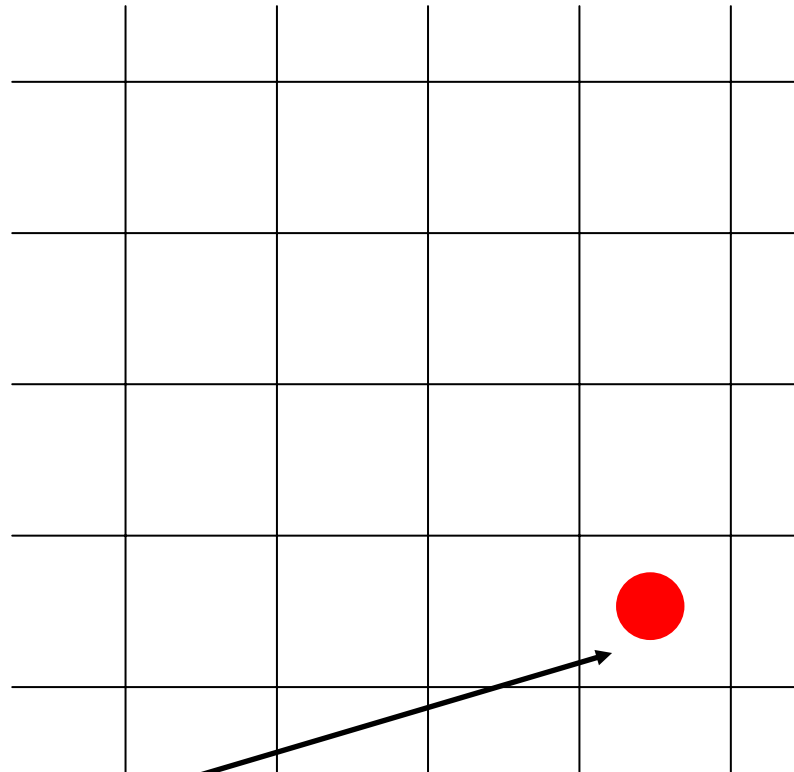


outcome that maximises
Nash product $u^B \times u^S$
in Lilac State

Red State

Soprano

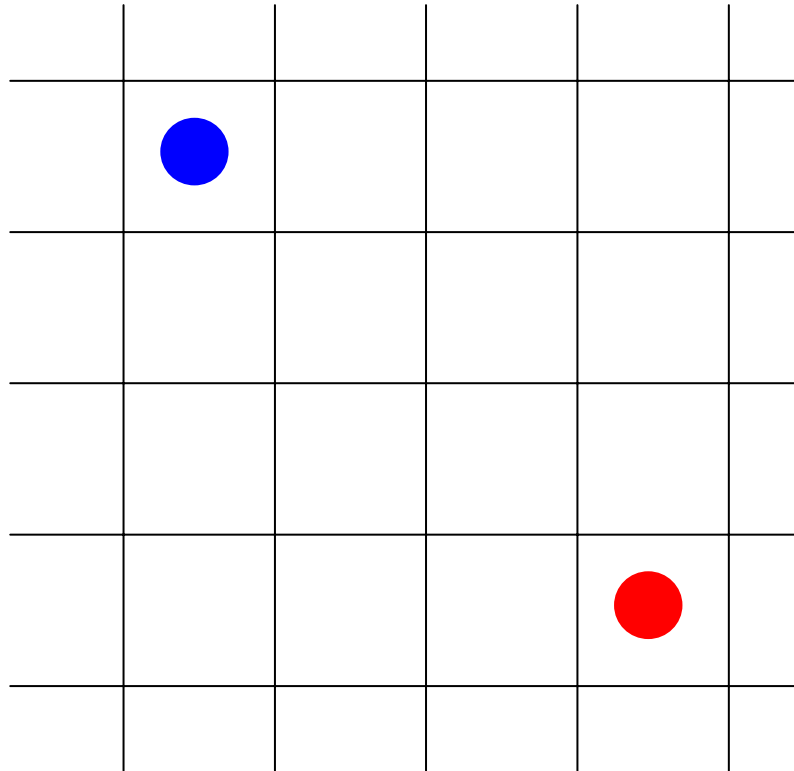
Bishop



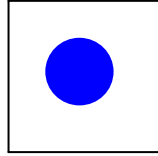
outcome that maximises
Nash product $u^B \times u^S$
in Red State

Soprano

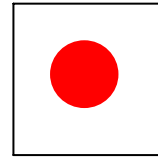
Bishop



Soprano



Bishop



$$C = \{ \bullet, \bullet \}$$

New way to think about contracts:

- contracts do rule out
pairs not in C cannot be
selected at date 1

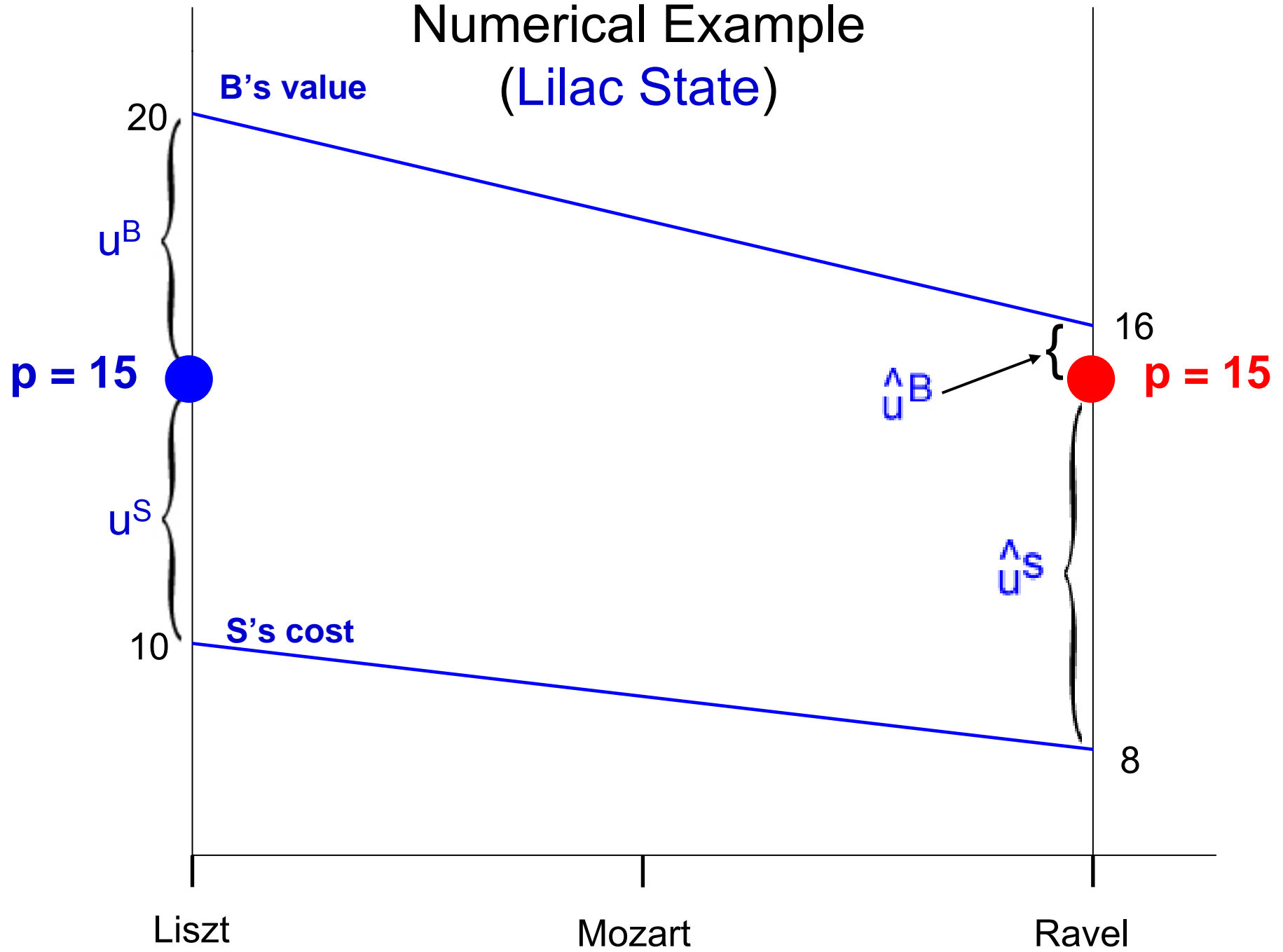
New way to think about contracts:

- contracts do rule out
pairs not in C cannot be
selected at date 1: no renegotiation

but

- contracts do not rule in
no mechanism is stipulated for
selecting a pair in C

Numerical Example (Lilac State)



Thus if p and p split date 1 surplus equally:

in **Lilac State** parties choose Liszt
(efficient!)

and, symmetrically,

in **Red State** parties choose Ravel
(efficient!)

Actually, these music/price pairs are the equilibrium outcomes from “No Contract”

Unequal split of date 1 surplus?

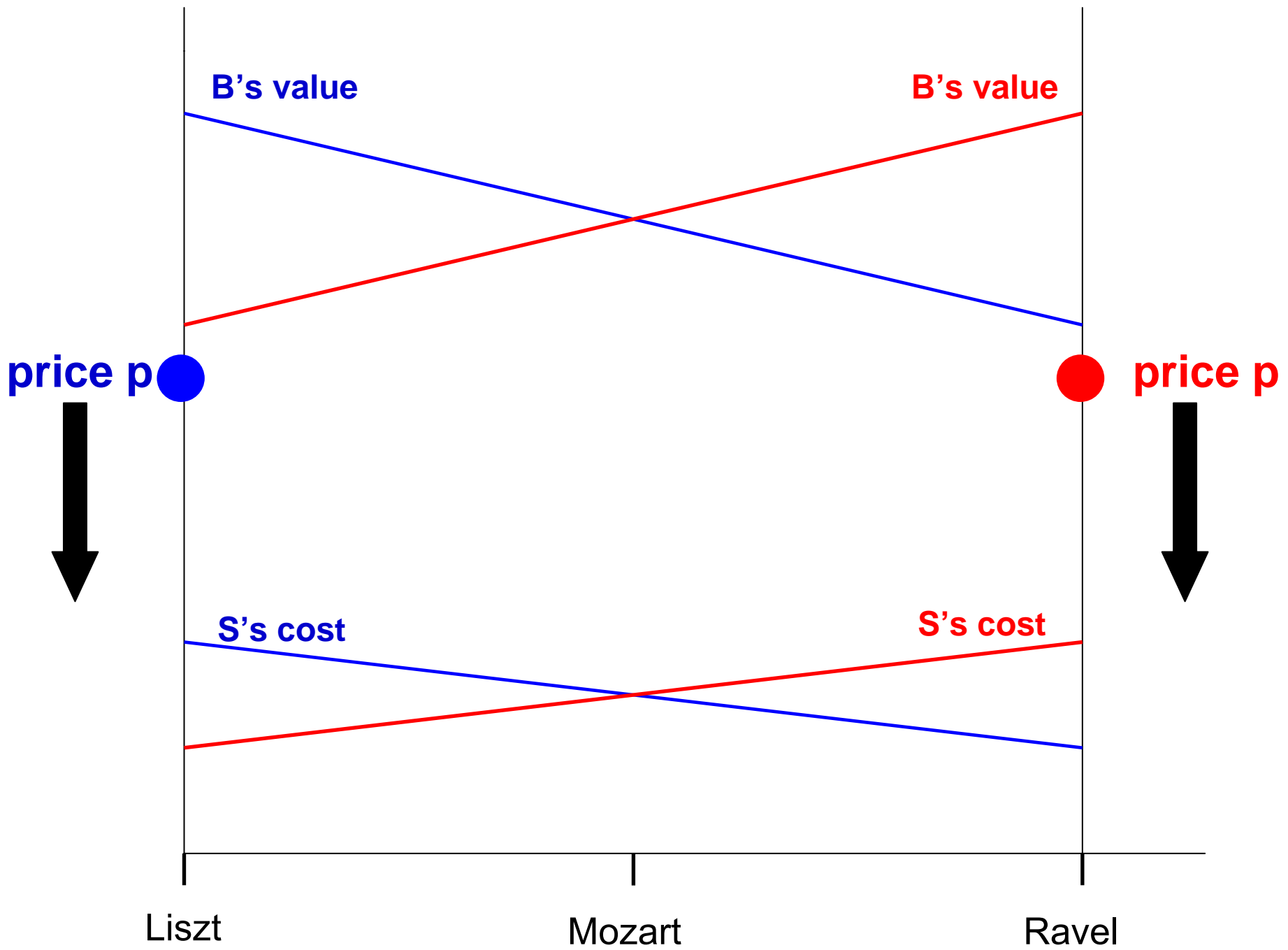
e.g. at date 0, the parties need a higher u^B

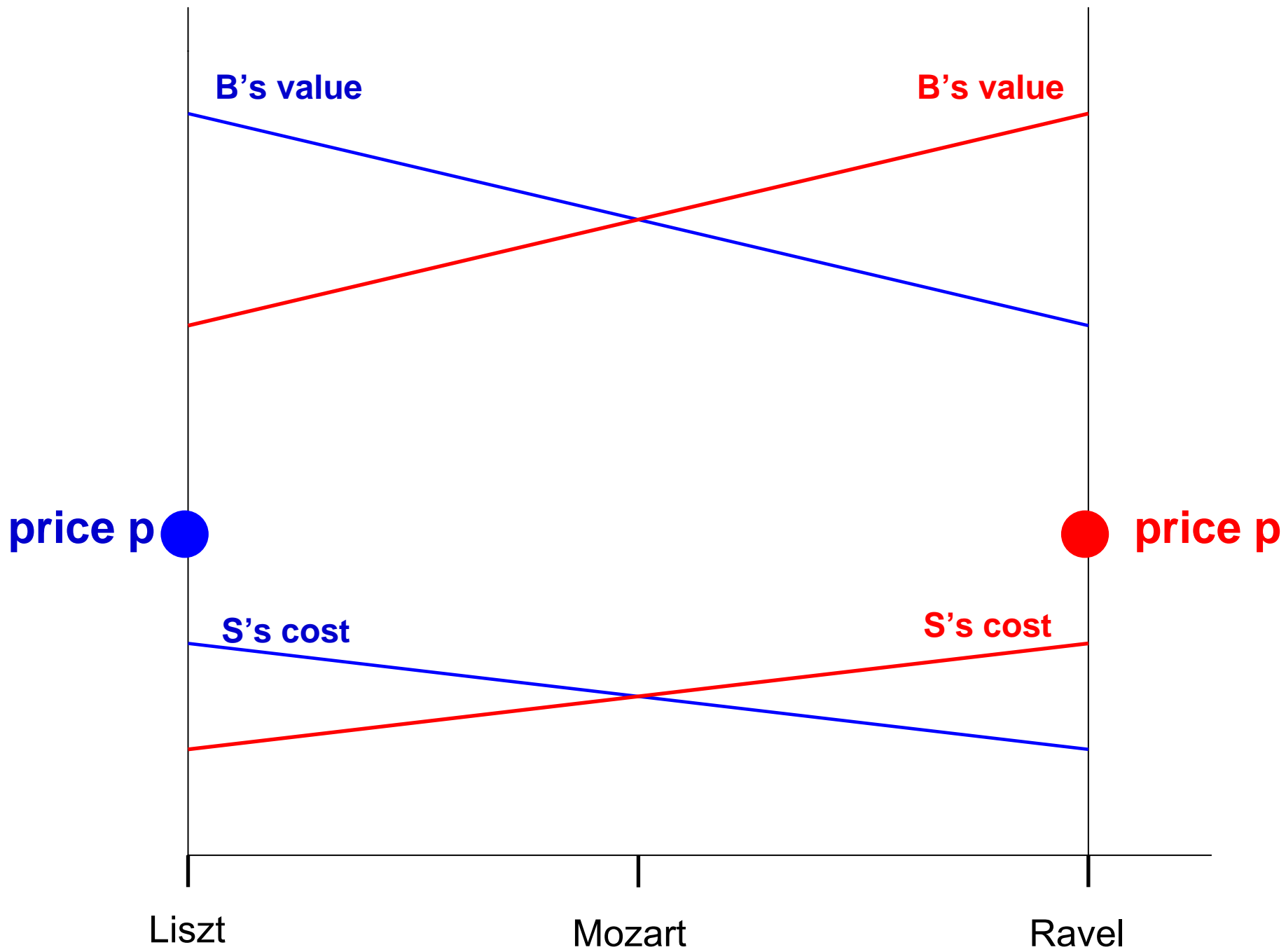
- the Bishop may have to make a non-contractible, relationship-specific investment at date $\frac{1}{2}$; and u^B must be enough to cover his sunk cost
(in this investment model, Judge cannot distinguish firing from quitting)

Unequal split of date 1 surplus?

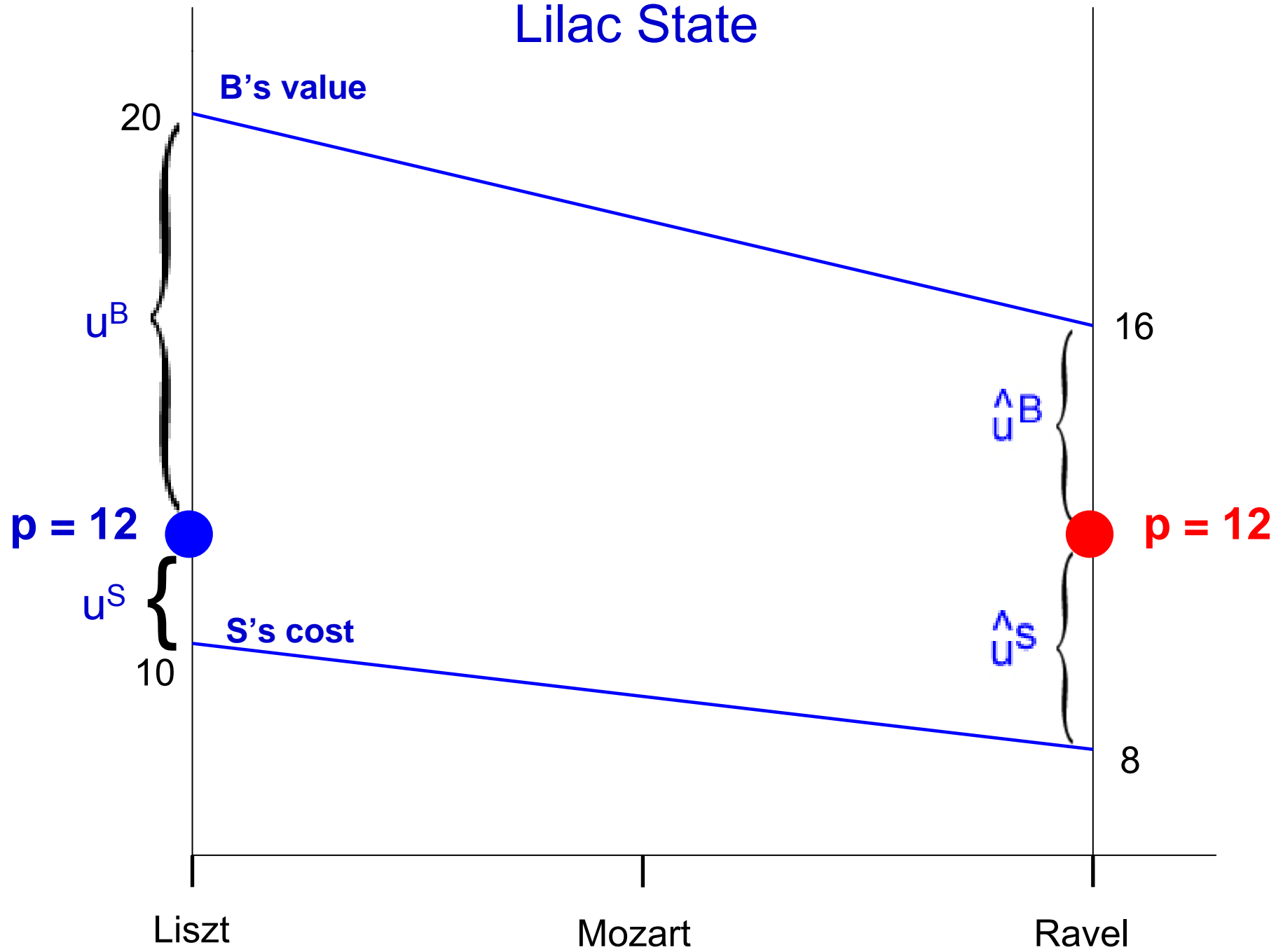
e.g. at date 0, the parties need a higher u^B

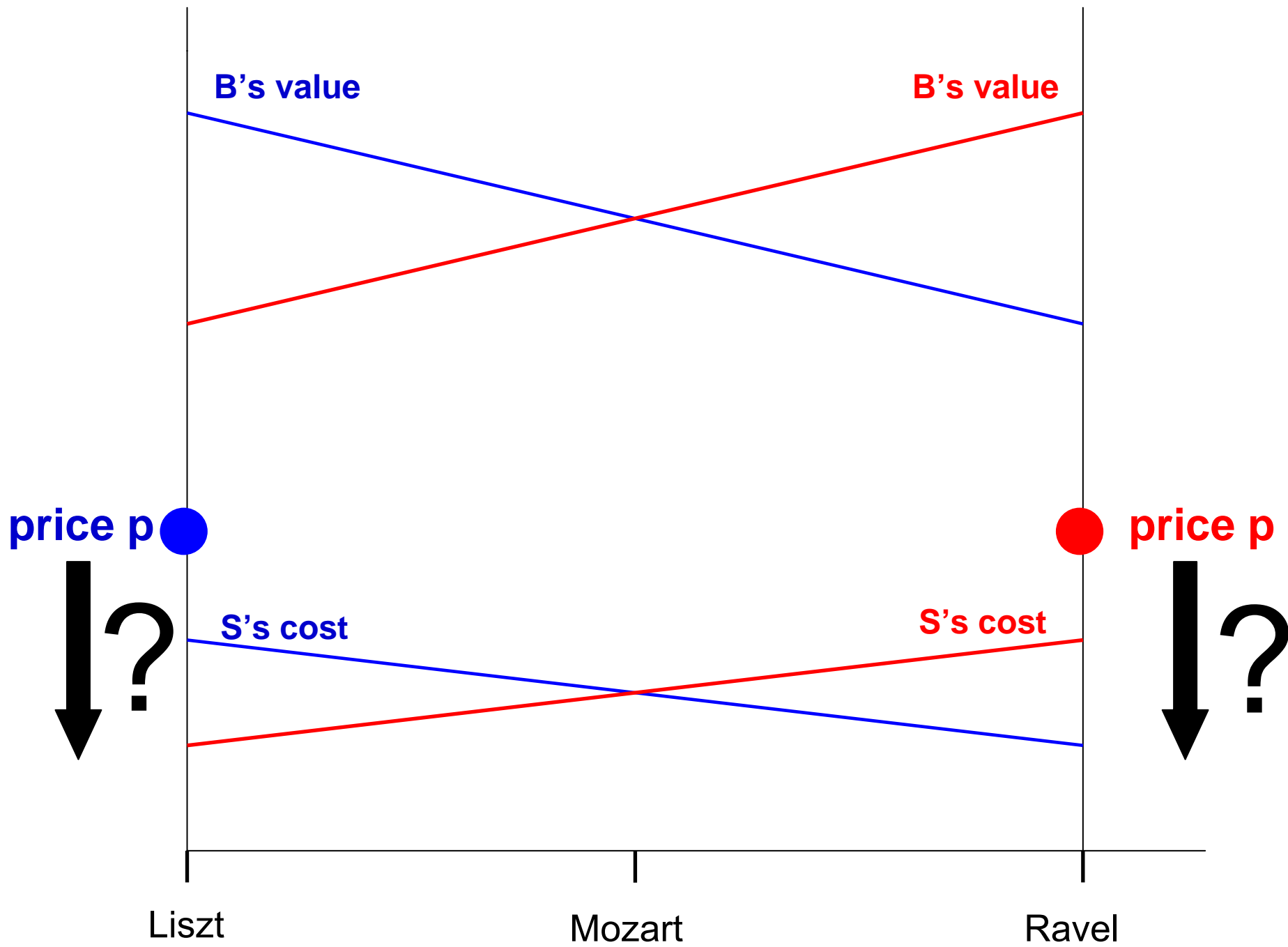
- the Bishop may have to make a non-contractible, relationship-specific investment at date $\frac{1}{2}$; and u^B must be enough to cover his sunk cost
- date 0 market-clearing price may be low (any upfront payment is part of “price”)

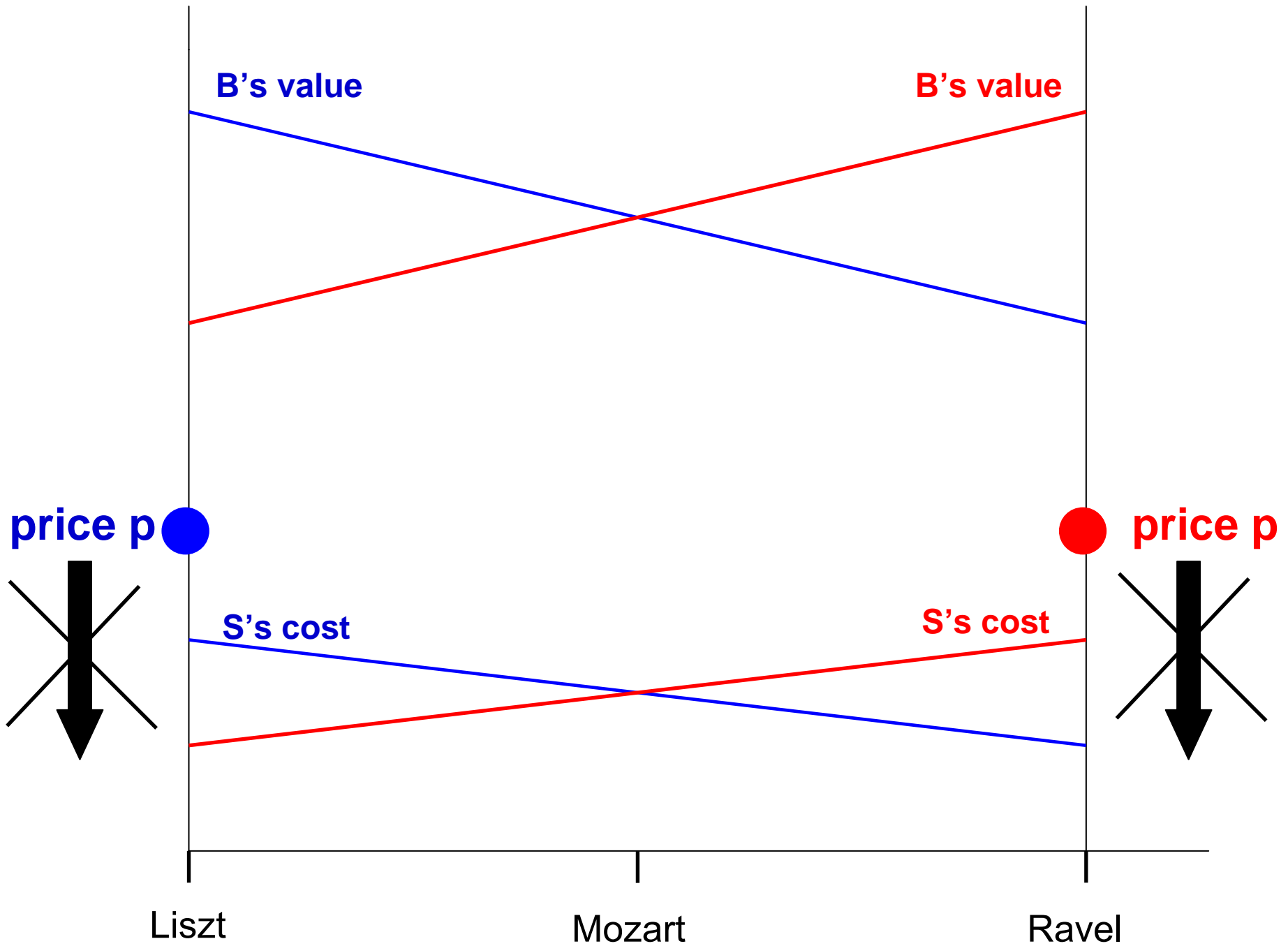


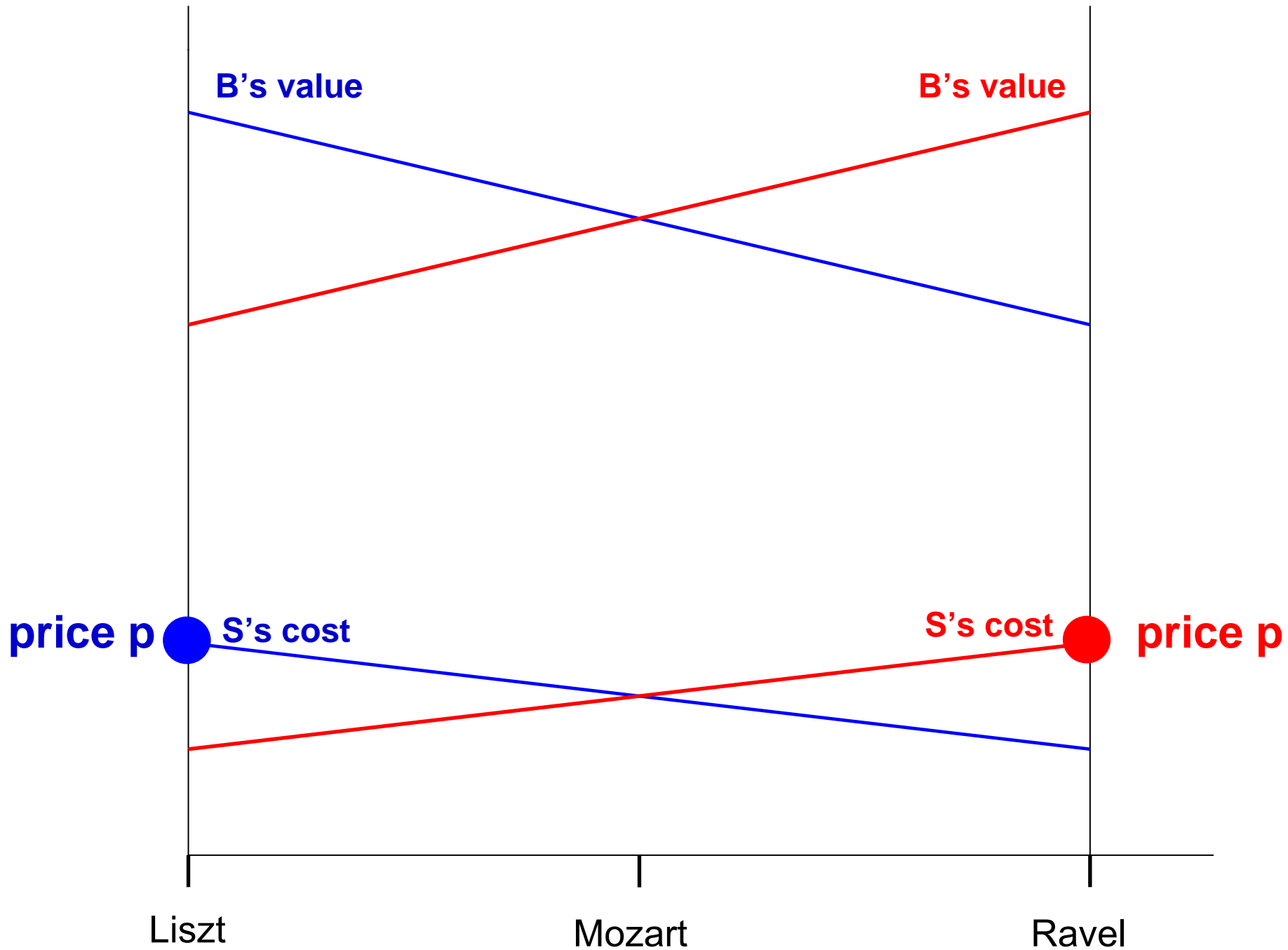


Lilac State

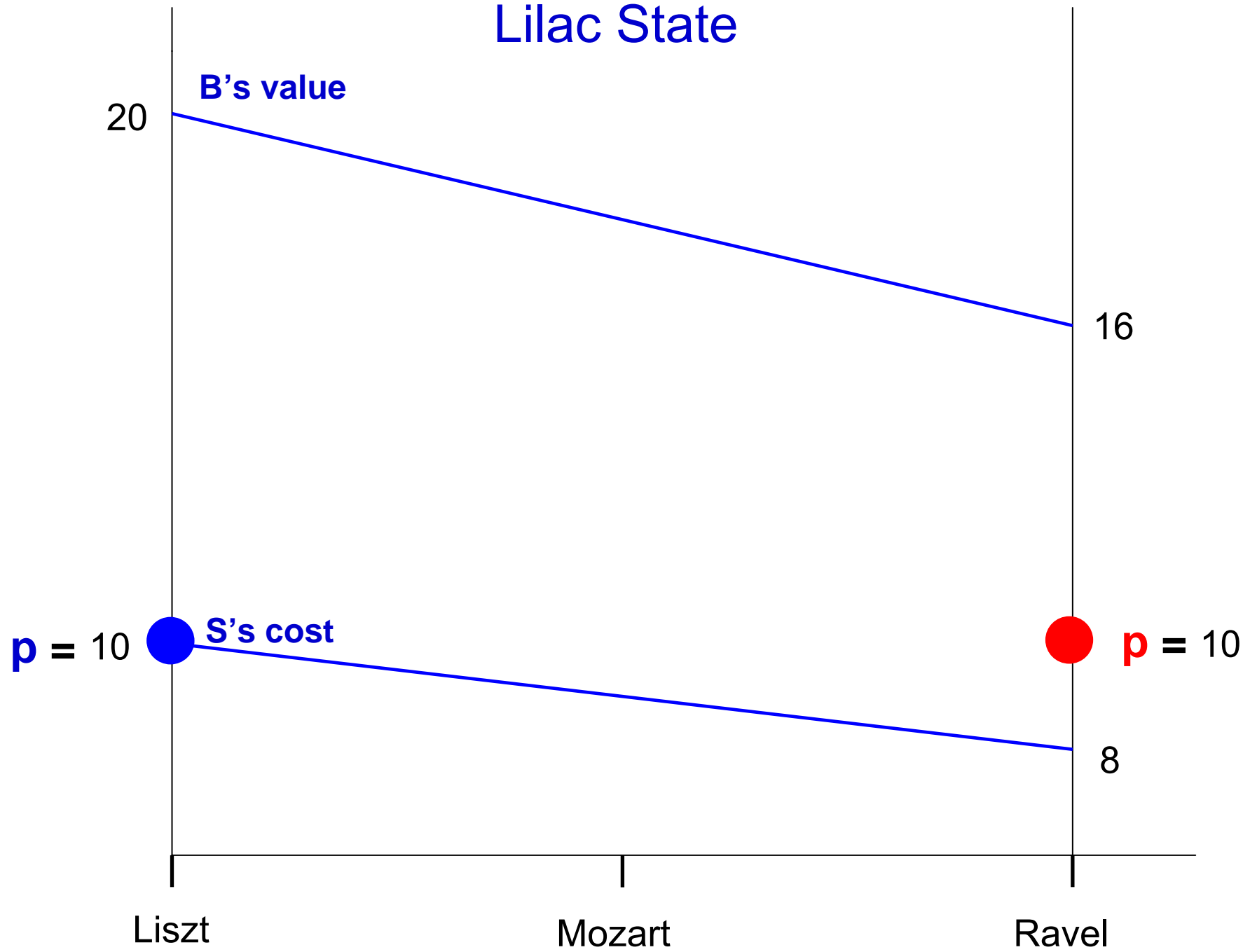




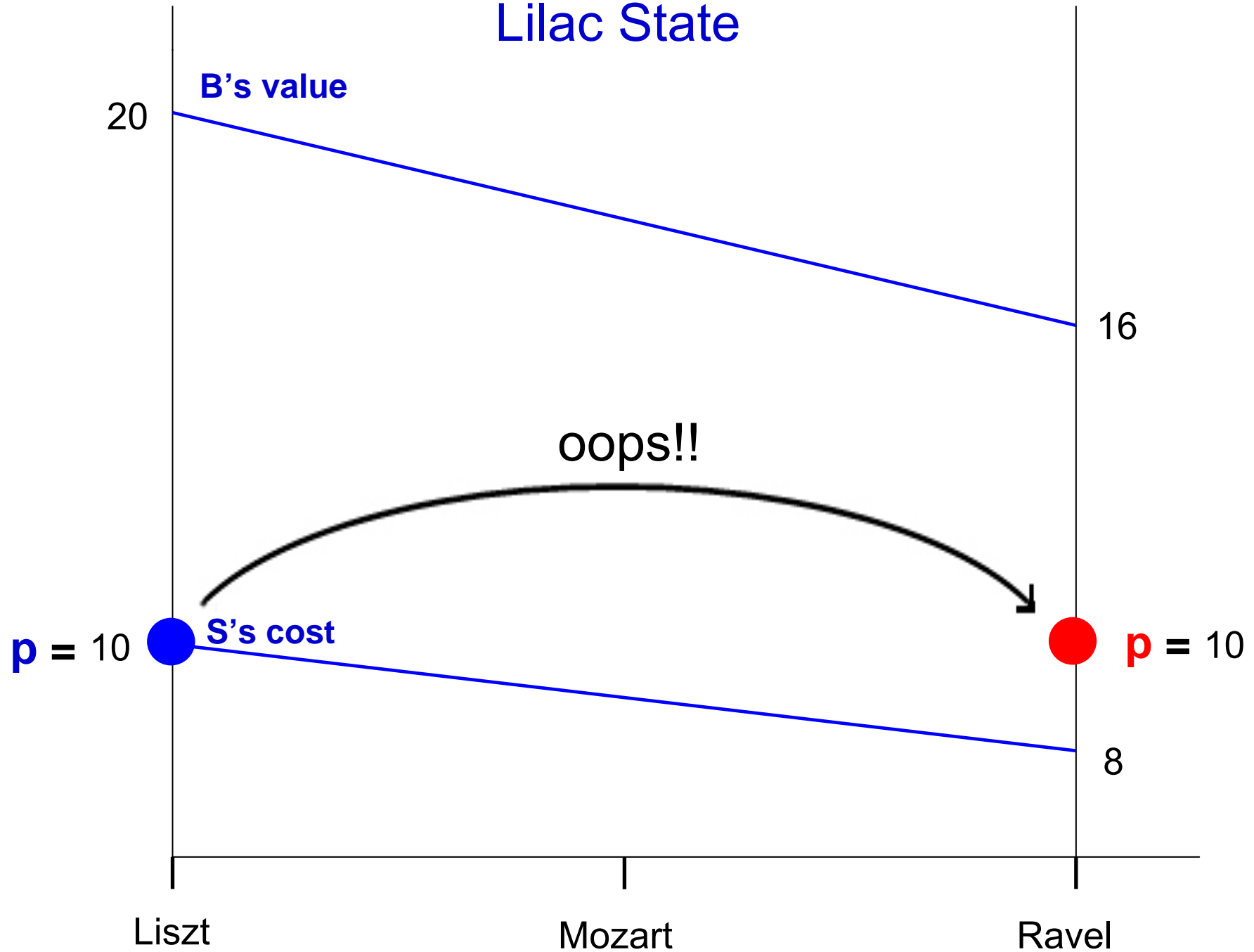




Lilac State



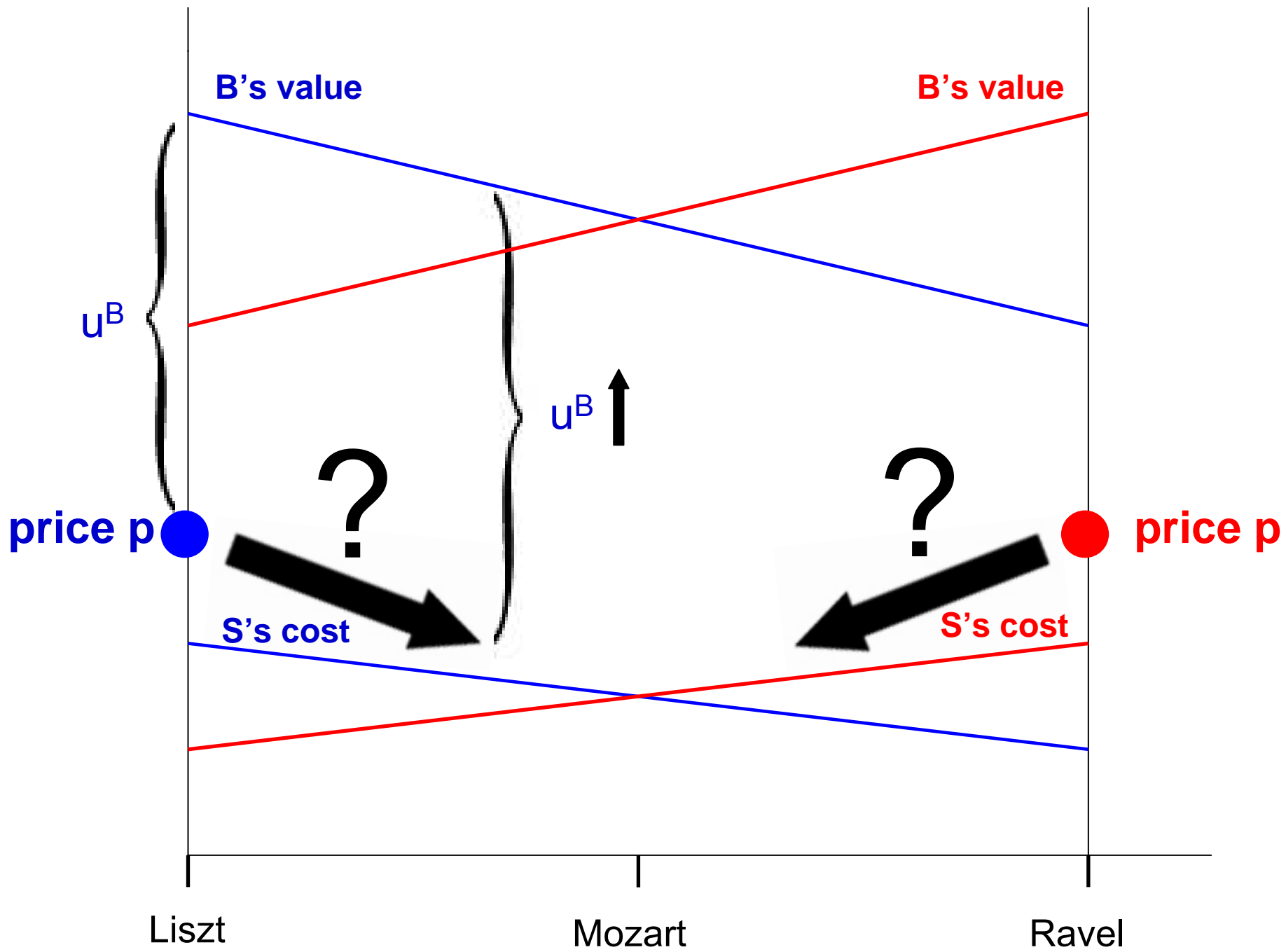
Lilac State

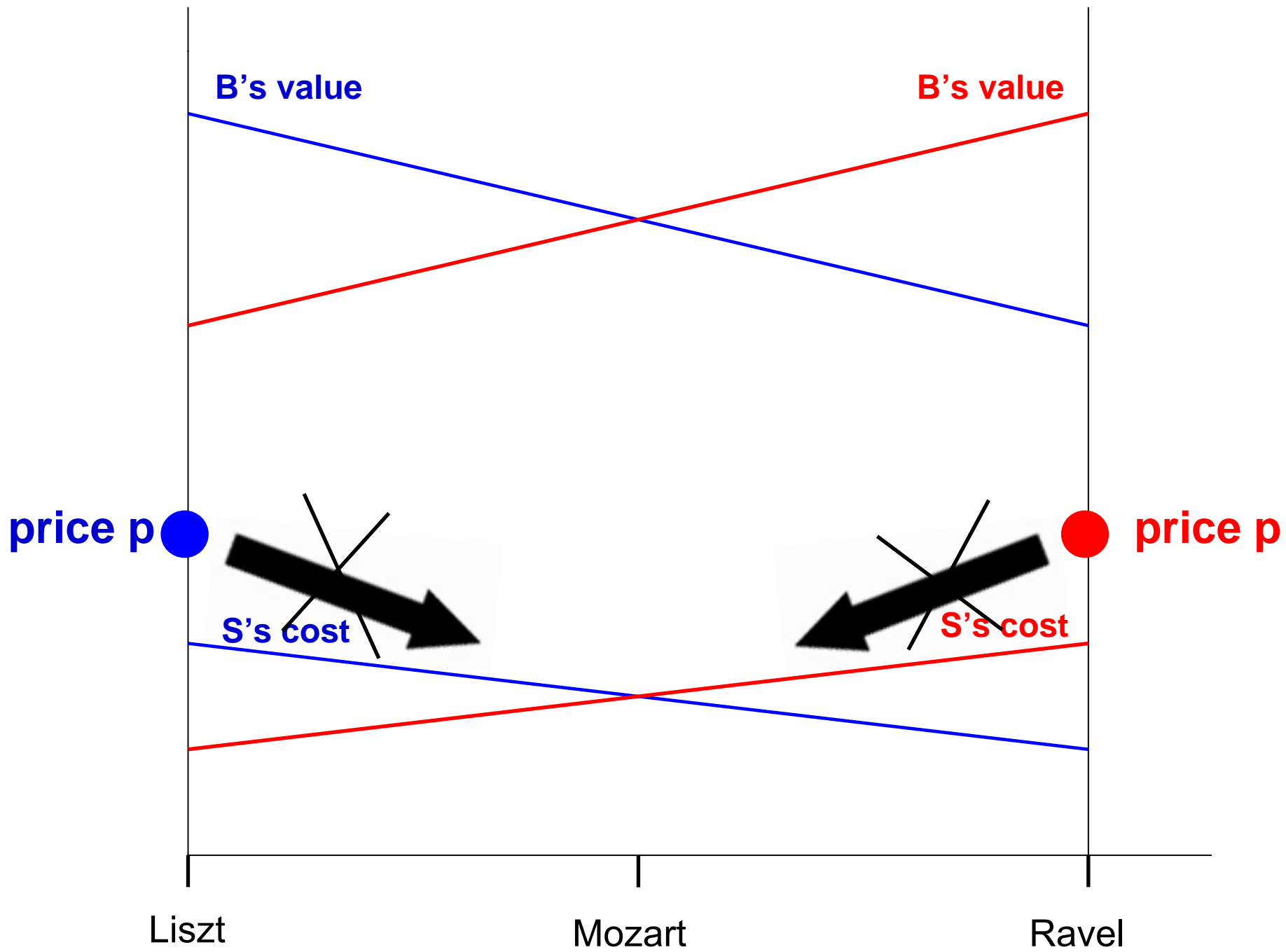


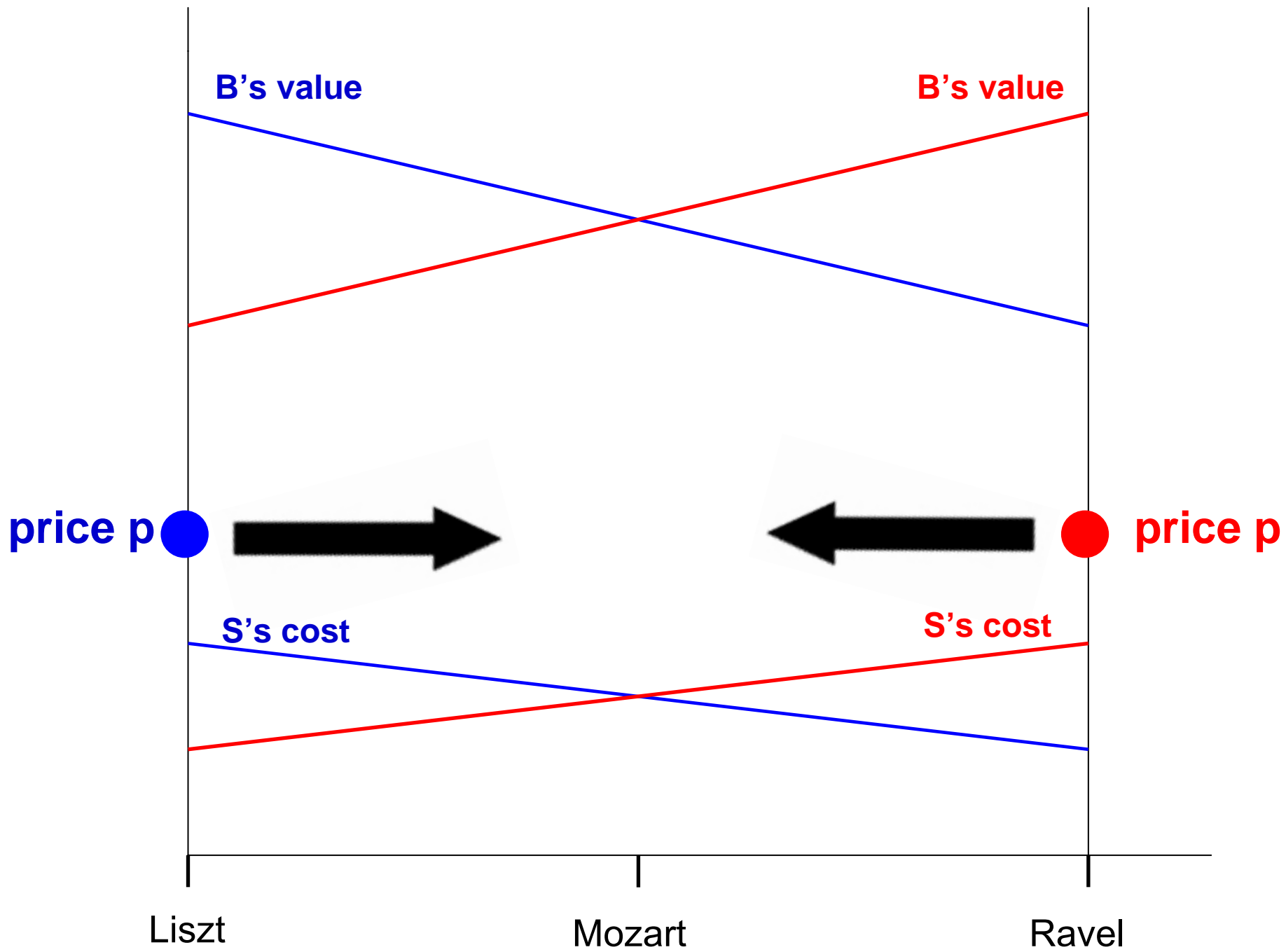
If p and p are set at too low a level,
the parties choose the least efficient music

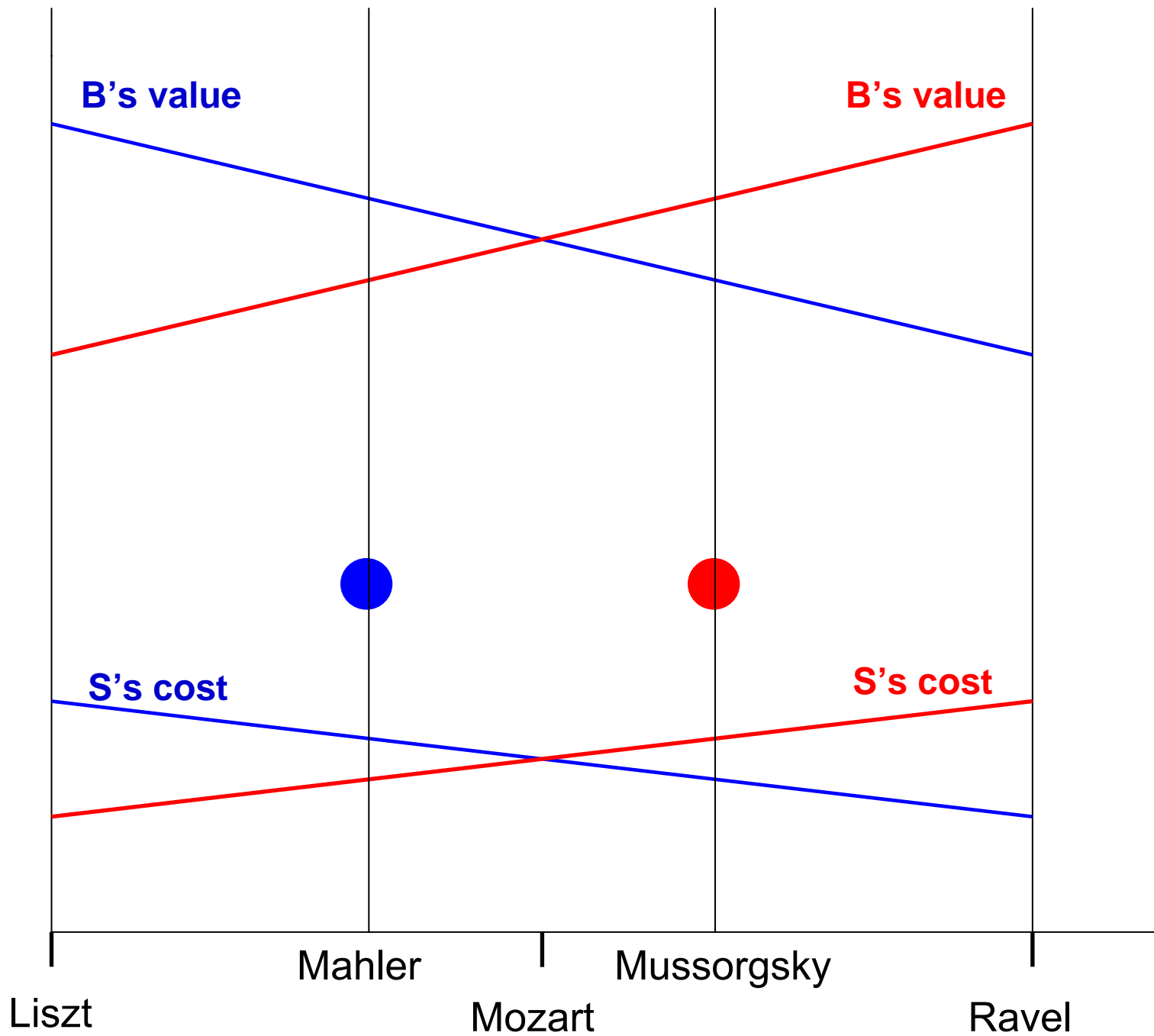
This would be worse than simply fixing the
music (at Liszt, say)

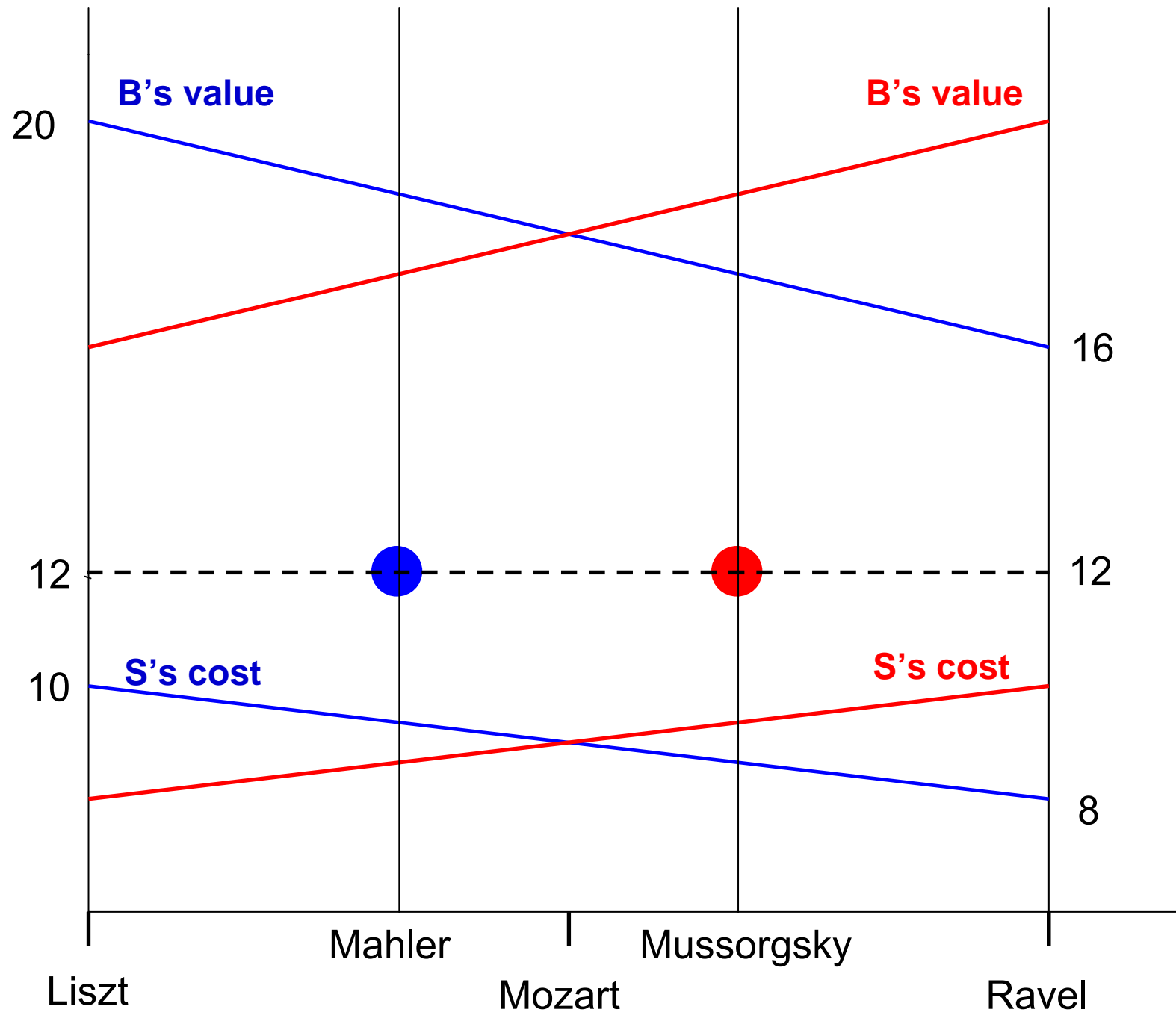
Let's try somewhat less efficient music ...







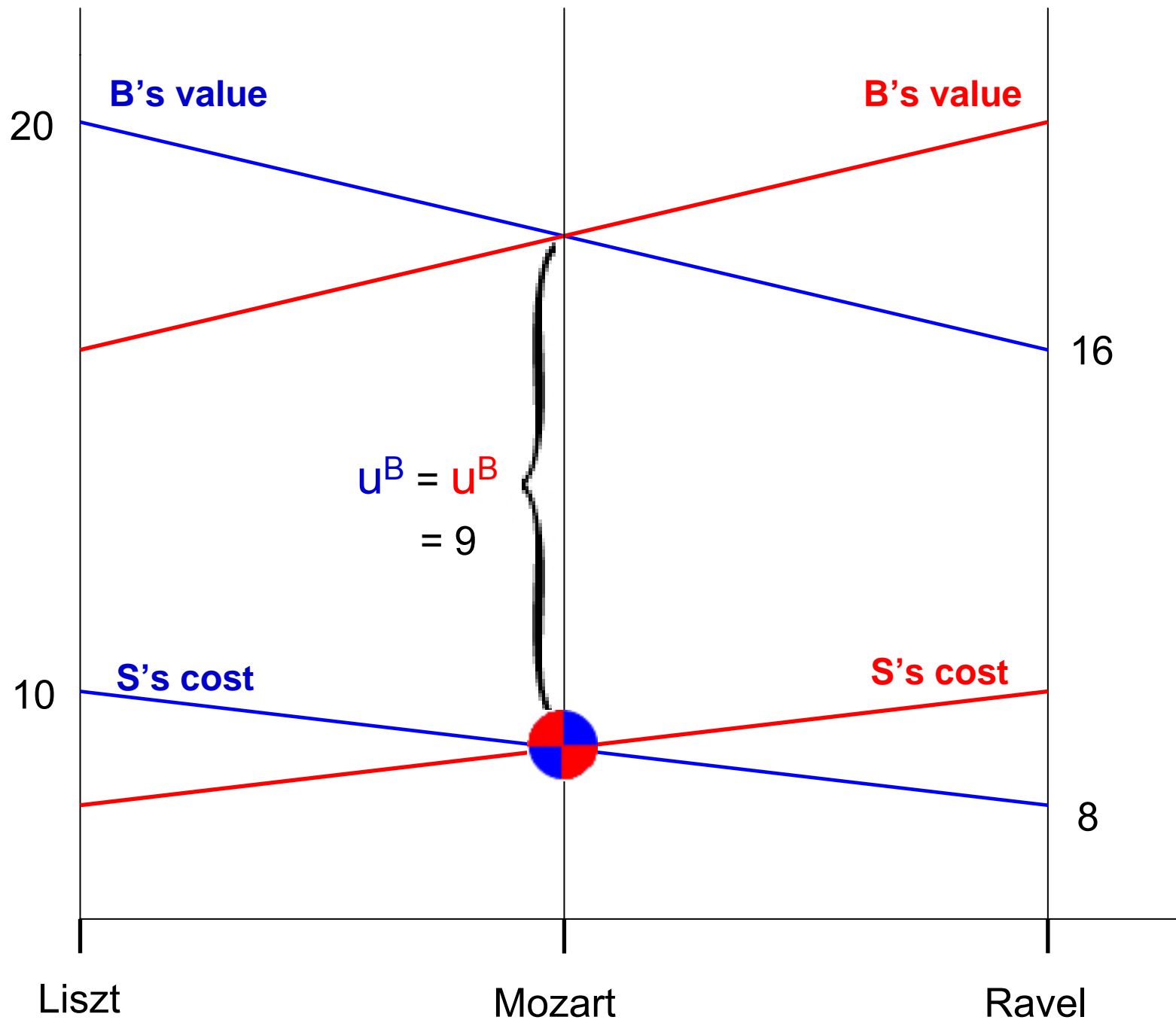




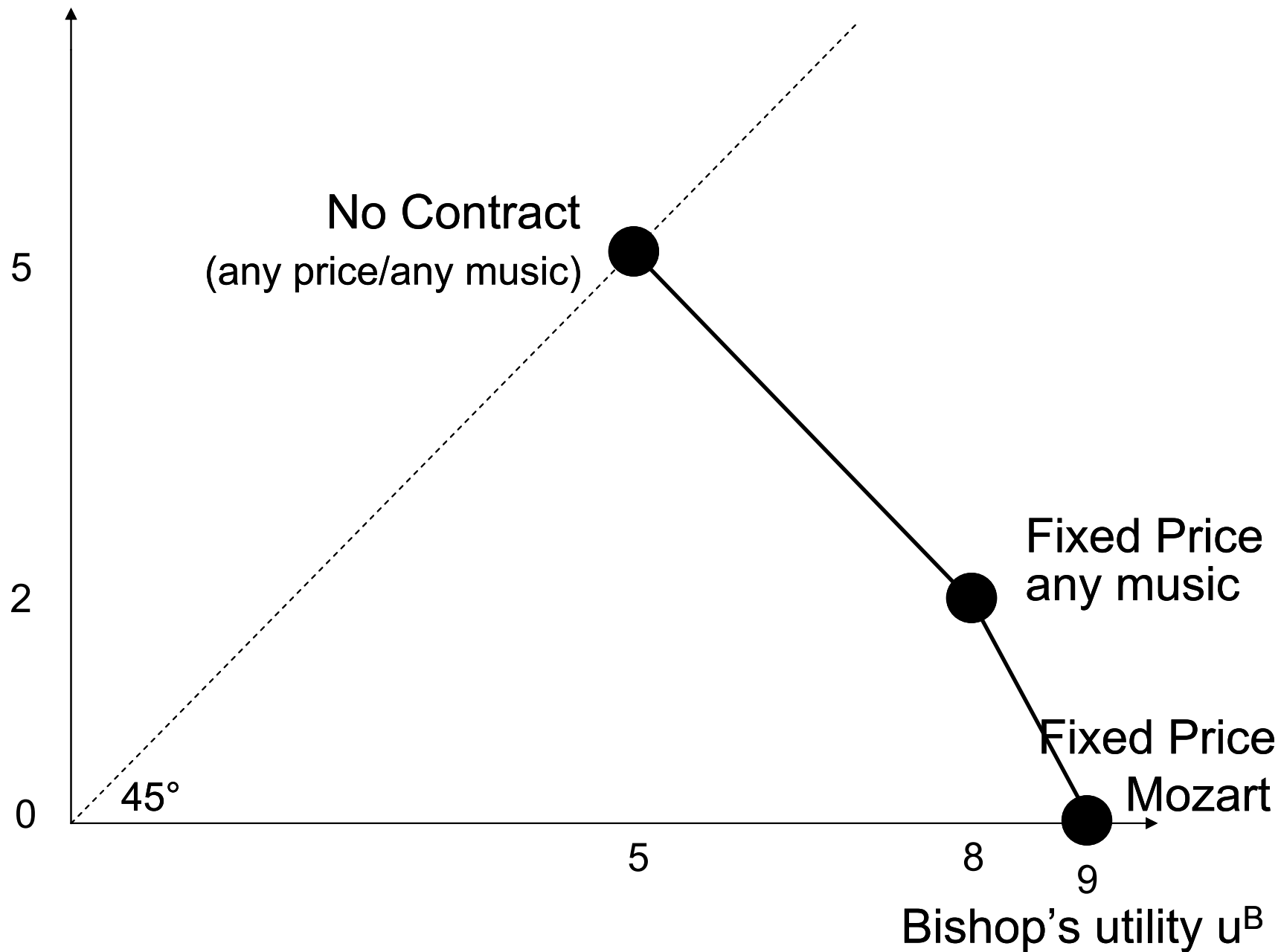
Unfortunately things are getting worse ...

as we move away from the efficient music,
the Bishop's utility u^B is falling
(as, of course, are the gains from trade)

BUT there is a discontinuity at Mozart!



Soprano's utility u^S



The discontinuity arises as we reduce the dimensionality of C from one to zero:

from two spots (● and ●)

to one spot (●)

More can be less!

Flexibility vs. rigidity:

flexibility (● and ●)

=> more efficiency at date 1

rigidity (⊕)

=> less opportunism at date 1

Order:

any price/any music



fixed price/any music



fixed price/fixed music

Never optimal to fix the music without fixing the price

Order:

any price/any music



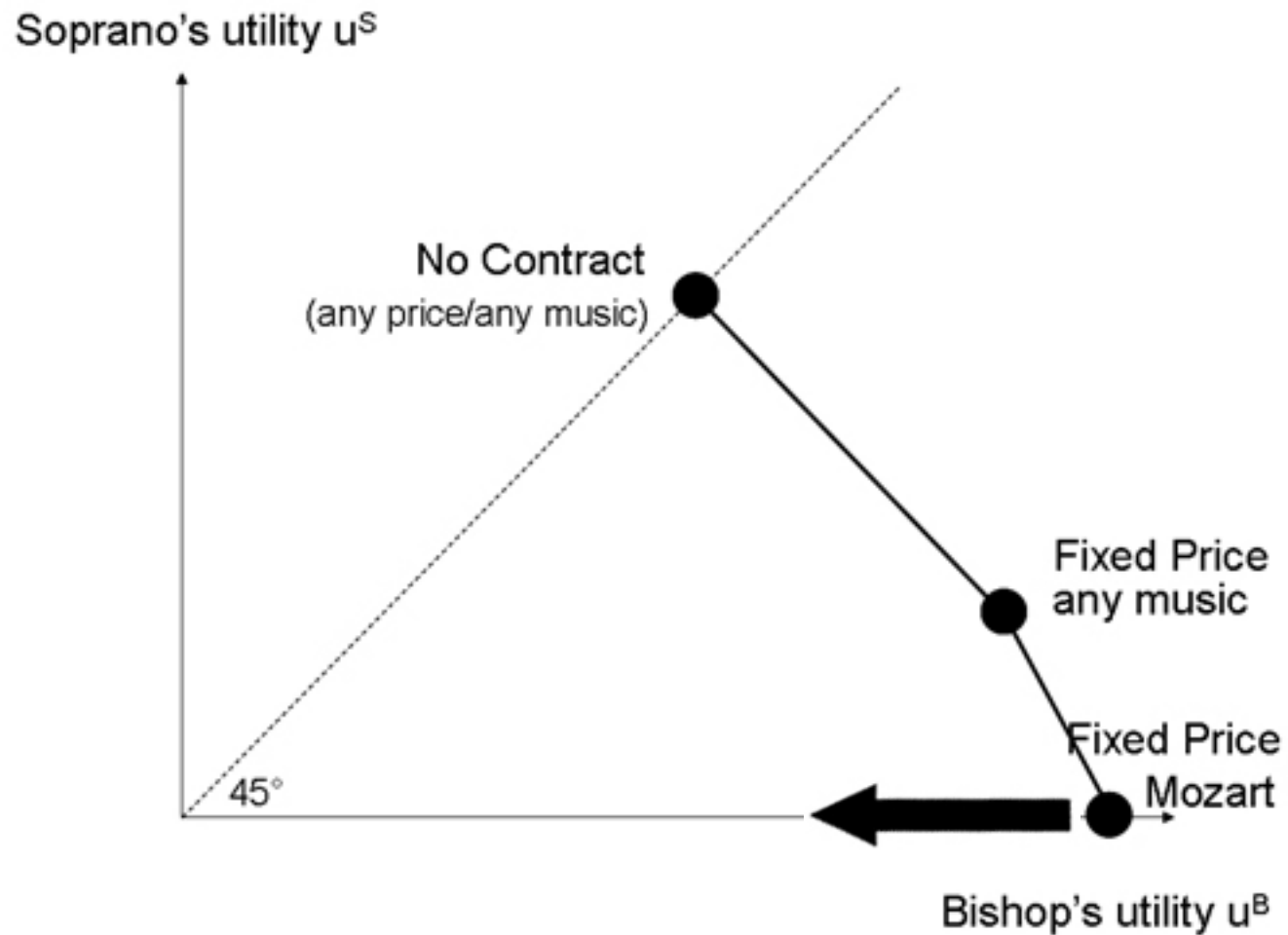
fixed price/any music



~~fixed price/fixed music~~

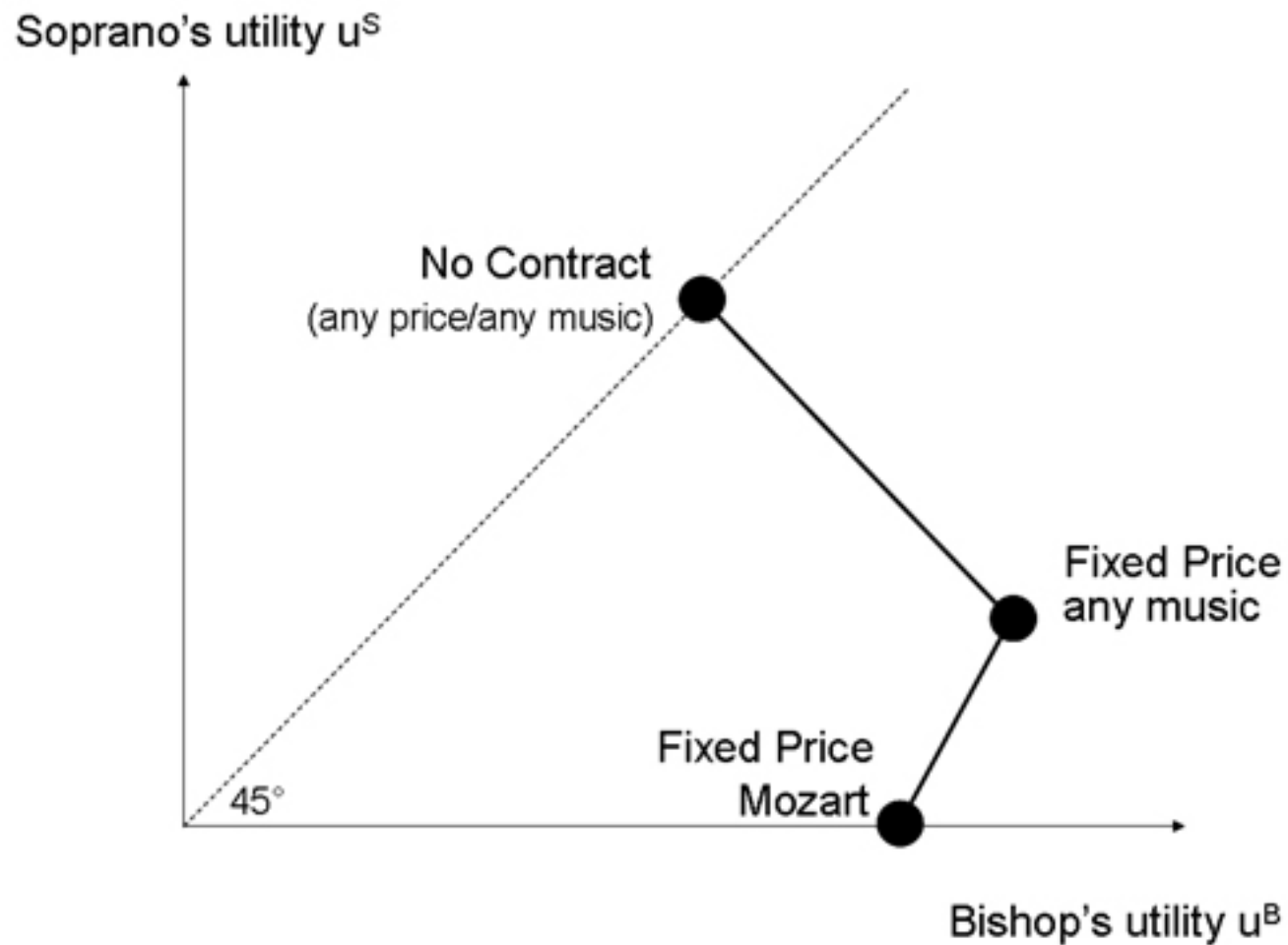
(for other parameter values)

Efficiency wages:



(for other parameter values)

Efficiency wages:



Keynes?

Employment contracts

Fixed price/any music $\stackrel{?}{=}$ employment

B and S bargain over choice of music:
they have a common view of what is fair

(Even if B has the “legal right” to choose,
it is a right in name only)

Have we gone too far?

Can't bosses tell subordinates what to do
– at least within reason?

More generally, contracts do stipulate
mechanisms for selecting outcomes,

i.e. contracts do rule in,
– at least to some extent

PAPER 2: “Contracts as Reference Points” (Hart-Moore, July 2006)

Suppose parties do not have a common view of what is fair

We take extreme position:

in the absence of a contract,
each party feels entitled to all the surplus

Role of contract:

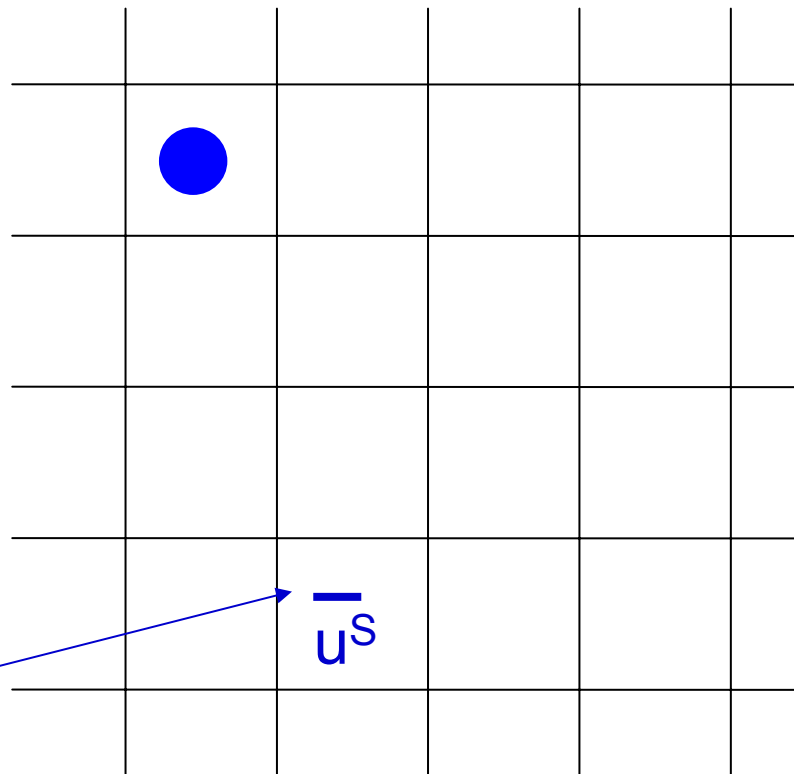
to limit parties' feelings of entitlement

Lilac State

Soprano

Bishop

S feels
entitled
to this



Role of contract:

to limit parties' feelings of entitlement

Lilac State

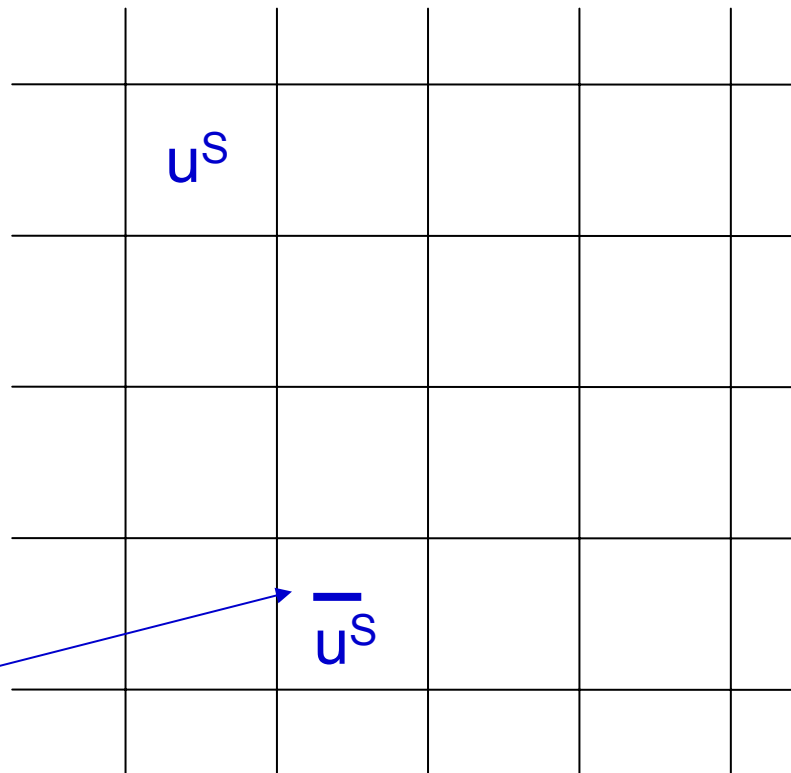
Soprano

S's aggrivement

$$= (\bar{u}^S - u^S)$$

Bishop

S feels
entitled
to this



Role of contract:

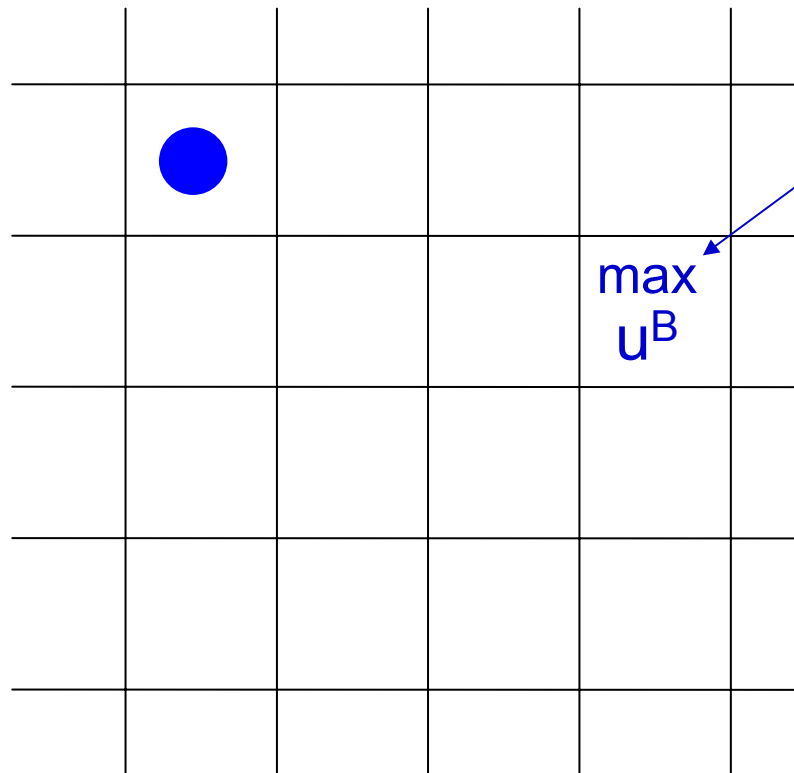
to limit parties' feelings of entitlement

Lilac State

Soprano

B feels entitled to this

Bishop



Role of contract:

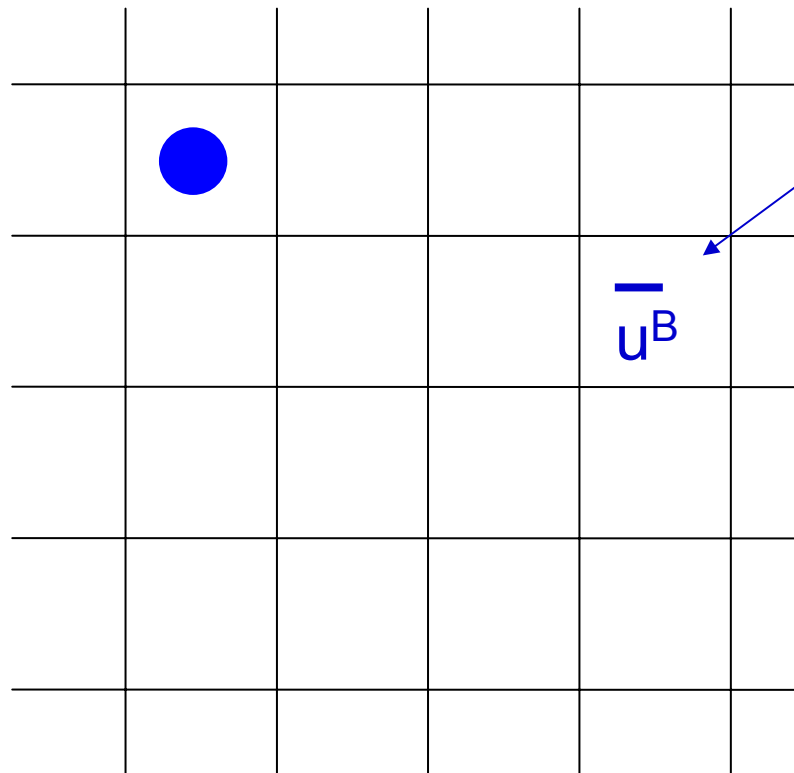
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Lilac State

Soprano

B feels entitled to this

Bishop



Role of contract:

to limit parties' feelings of entitlement

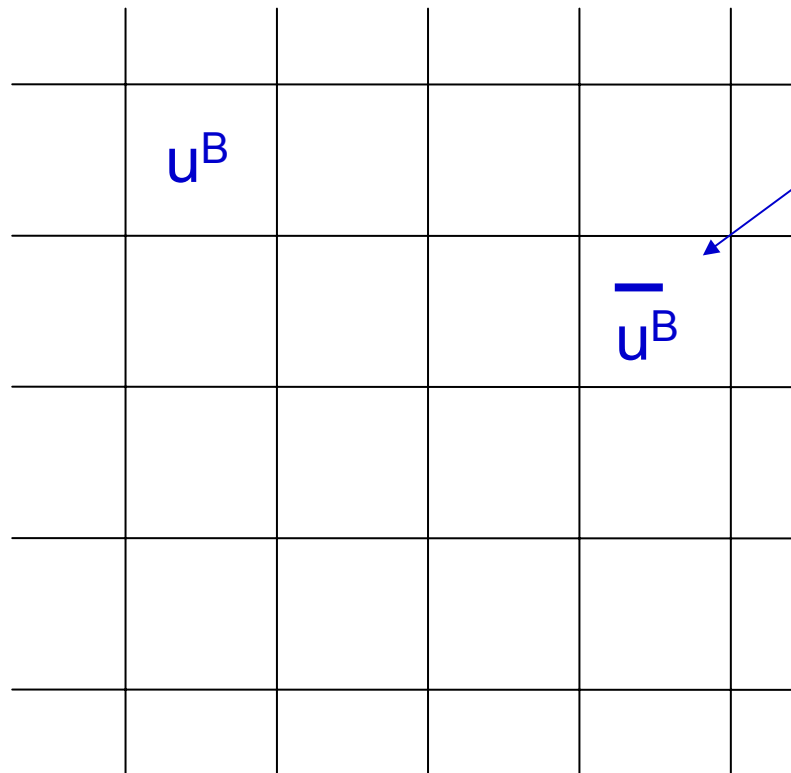
Lilac State

Soprano

B feels entitled to this

B's aggrievement
 $= (\bar{u}^B - u^B)$

Bishop



Assume: parties shade their performance in proportion to how aggrieved they feel

=> loss in **Lilac State** equals

$$\text{Loss} = \theta \{ \bar{u}^S - u^S \} + \theta \{ \bar{u}^B - u^B \}$$

constant of proportionality constant of proportionality

where $0 < \theta \leq 1$

Assume: parties shade their performance in proportion to how aggrieved they feel

=> loss in Lilac State equals

$$\text{Loss} = \underbrace{\theta \{ \bar{u}^S - u^S \}}_{\text{loss imposed on B by S's shading}} + \underbrace{\theta \{ \bar{u}^B - u^B \}}_{\text{loss imposed on S by B's shading}}$$

NB: own utility is unaffected by own shading

Role of contract:

to limit parties' feelings of entitlement

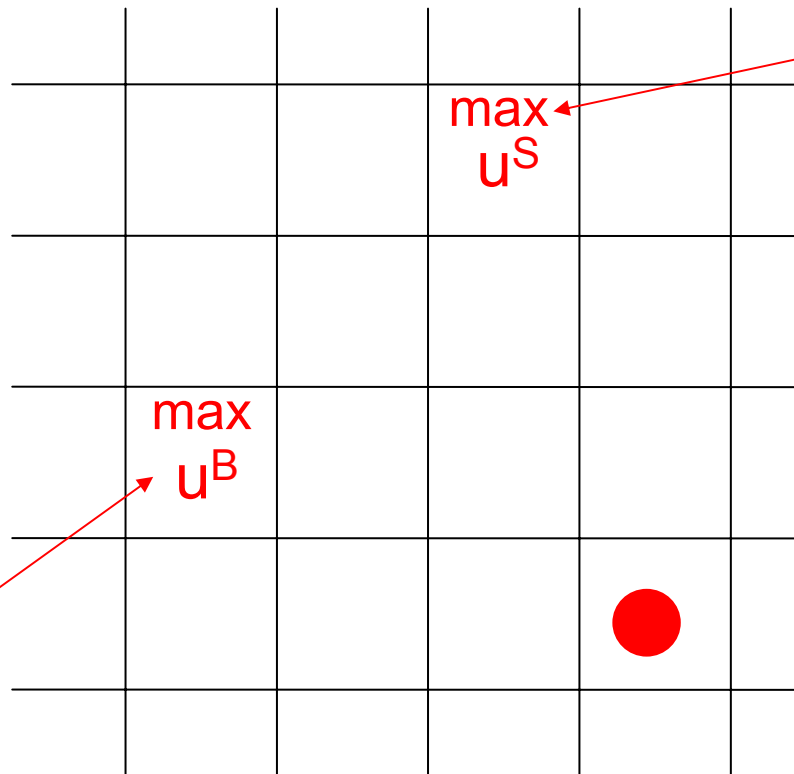
Red State

Soprano

S feels entitled to this

Bishop

B feels entitled to this



Role of contract:

to limit parties' feelings of entitlement

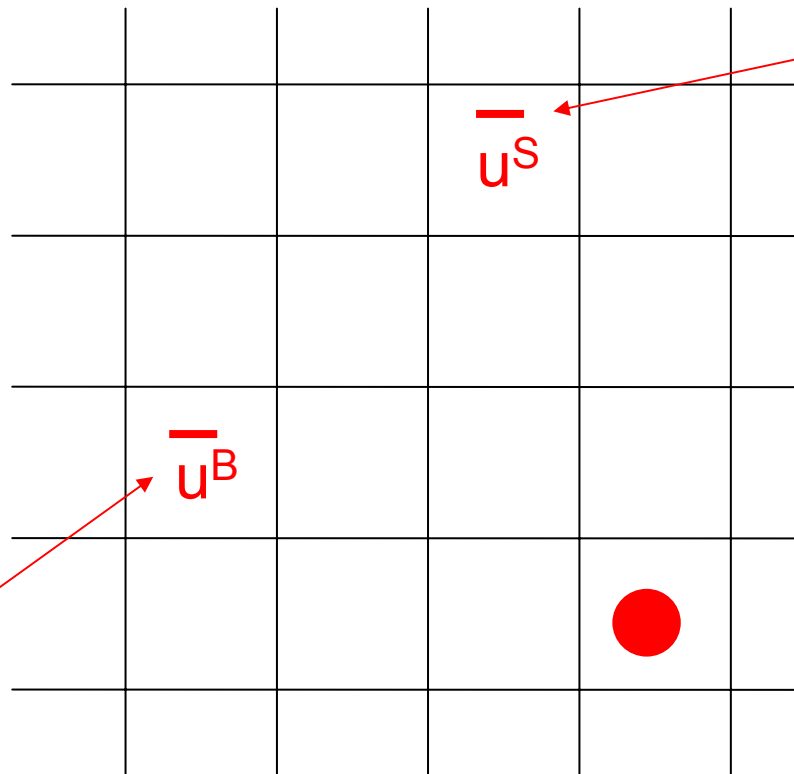
Red State

Soprano

S feels entitled to this

Bishop

B feels entitled to this



=> loss in **Red State** equals

$$\text{Loss} = \underbrace{\theta \{ \bar{u}^S - u^S \}}_{\text{loss imposed on B by S's shading}} + \underbrace{\theta \{ \bar{u}^B - u^B \}}_{\text{loss imposed on S by B's shading}}$$

Bring this machinery to Bishop/Soprano model:

for small θ ,

fixed price ($p = \bar{p}$)
Bishop chooses music

is the unique optimal contract

employment contract!

for large enough θ ,

fixed price ($p = p$)
fixed music (e.g. Mozart)

is the optimal

(in this case, more is less)

What is never optimal is “No Contract”:

any price
any music

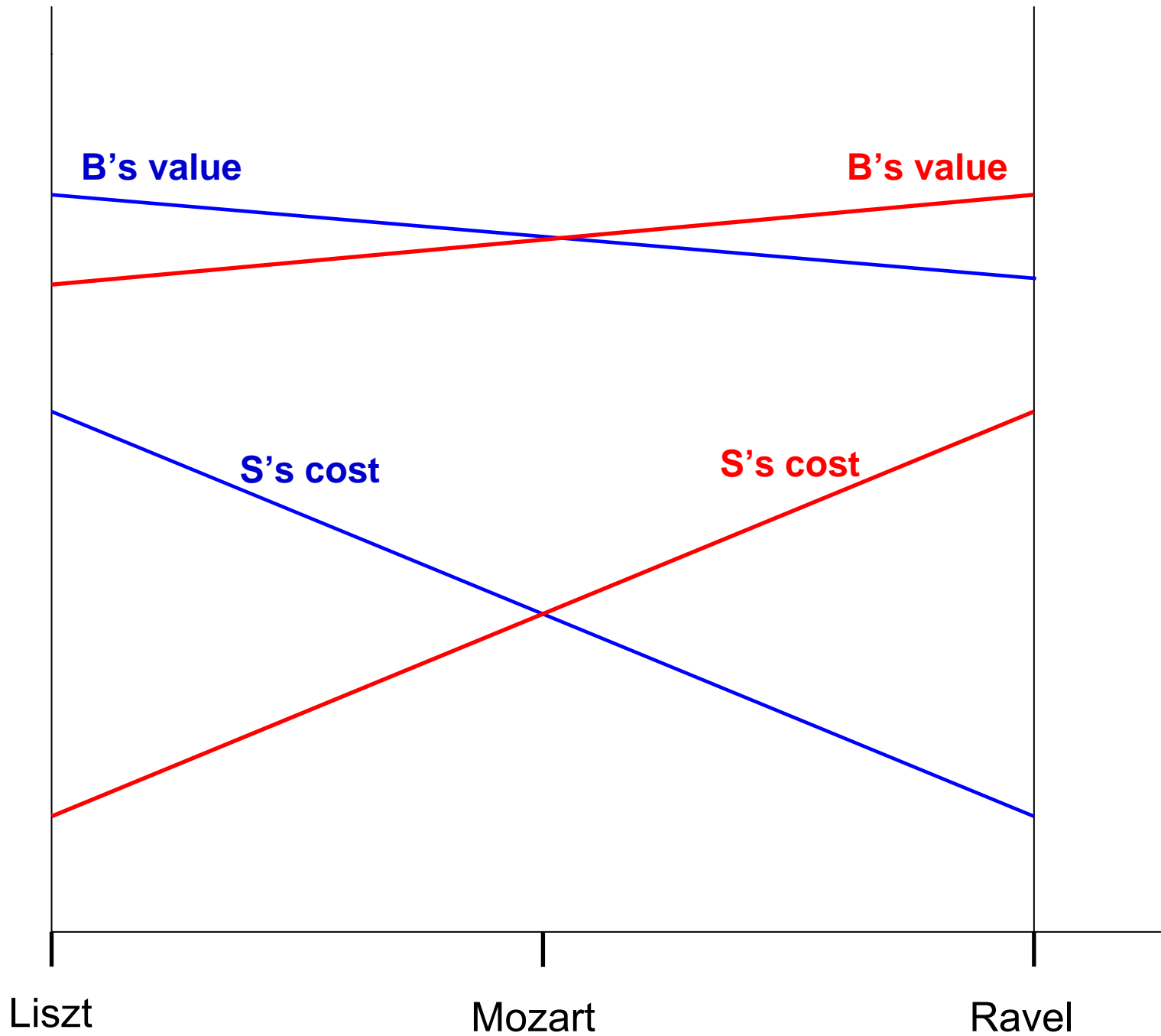
If price is not fixed at date 0, then at date 1
B and S will fight over money (as well as
music):

for every M euros fought over,
there will be a (combined) loss of θM

Also not optimal is “sub-contracting”:

fixed price ($p = p$)
Soprano chooses music

sub-contracting would be optimal if the
Soprano had more at stake than the Bishop:



Advantages of the machinery in PAPER 2, relative to PAPER 1:

- restores a role for mechanisms which we see in practice
 - e.g. employment contracts
 - distribution of surplus is unimportant
 - e.g. no need for specific investment
- => analysis is simpler

Arguably, disadvantage of PAPER 2,
relative to PAPER 1:

- relies on speculative psychological assumptions
(θ is an unmodelled free parameter)

But perhaps this is an advantage?

THE END